

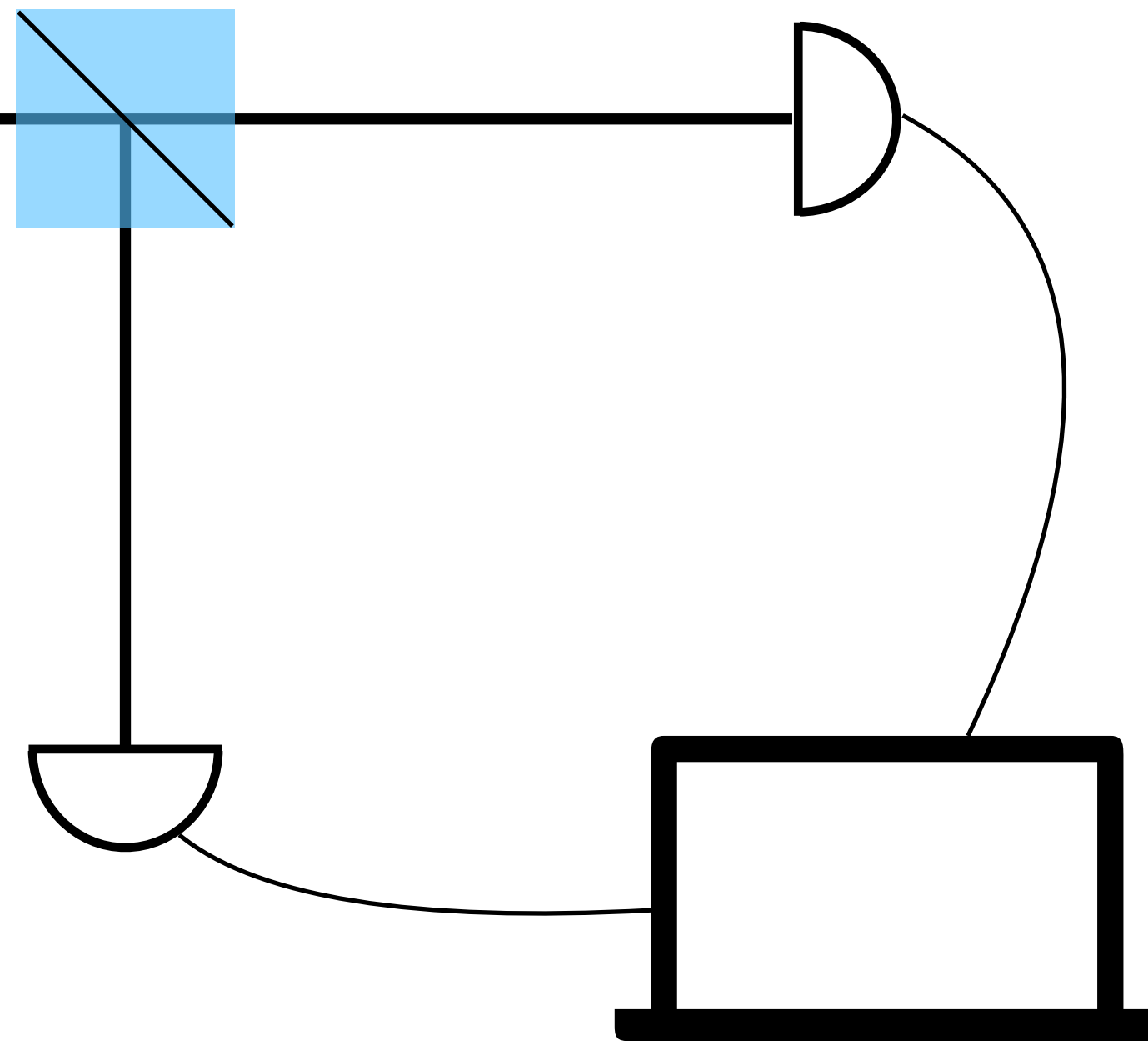
Bell, Wigner, causal reasoning, and interpretations

Andrea Di Biagio www.patternsthat abide.xyz
QISS Virtual Seminar 2025-06-19

Bell, Wigner

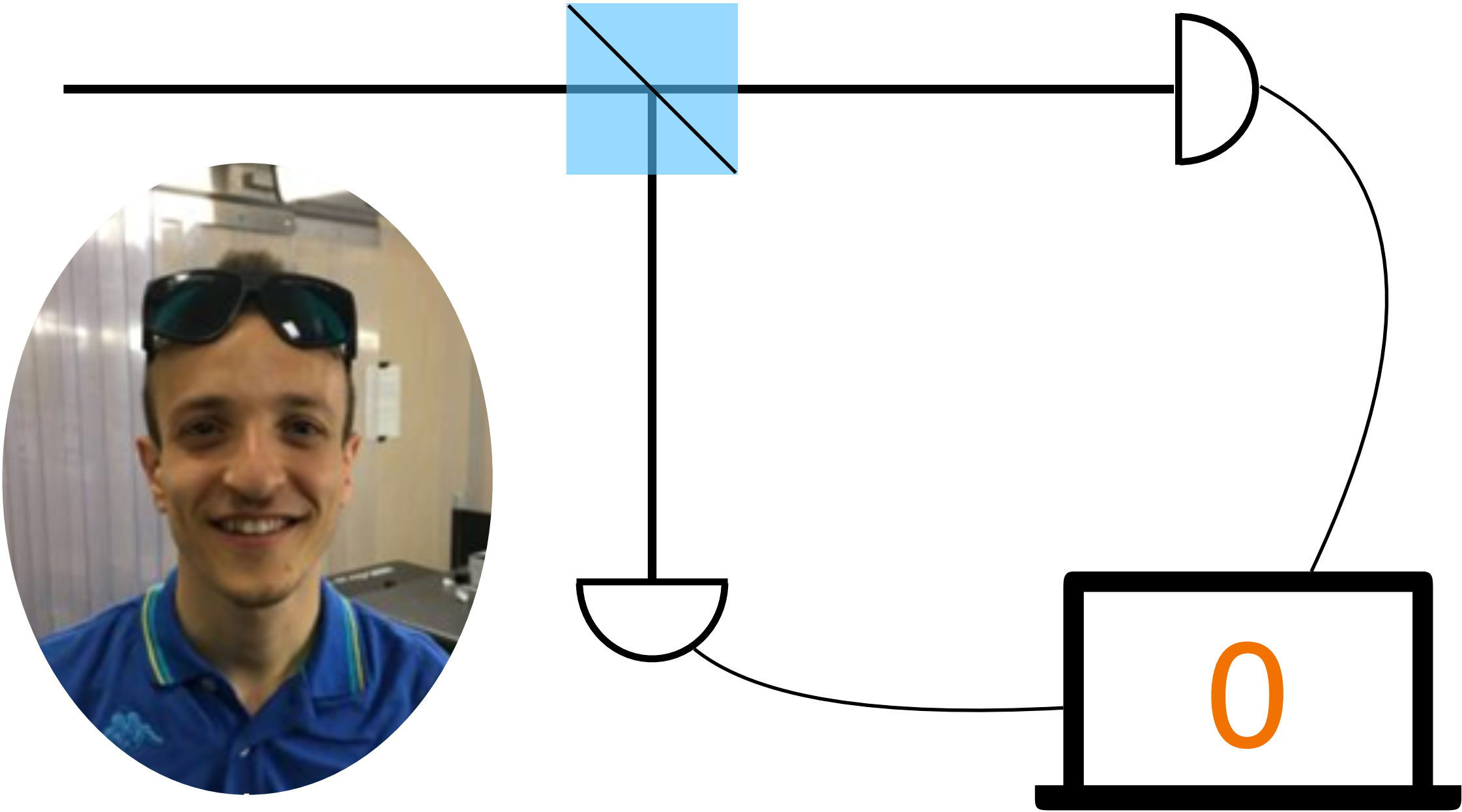
friends

$$\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle$$



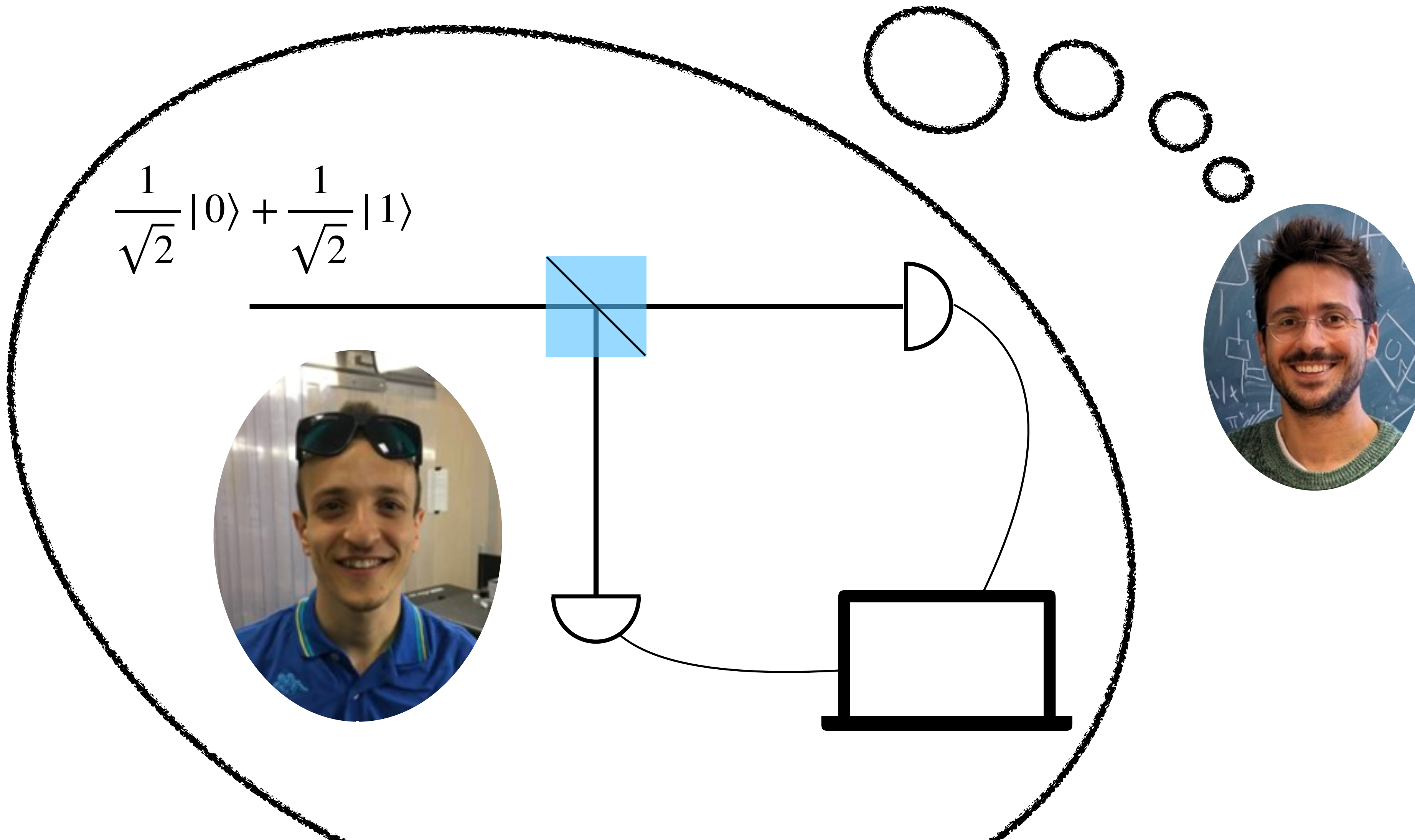
Bell, Wigner

friends



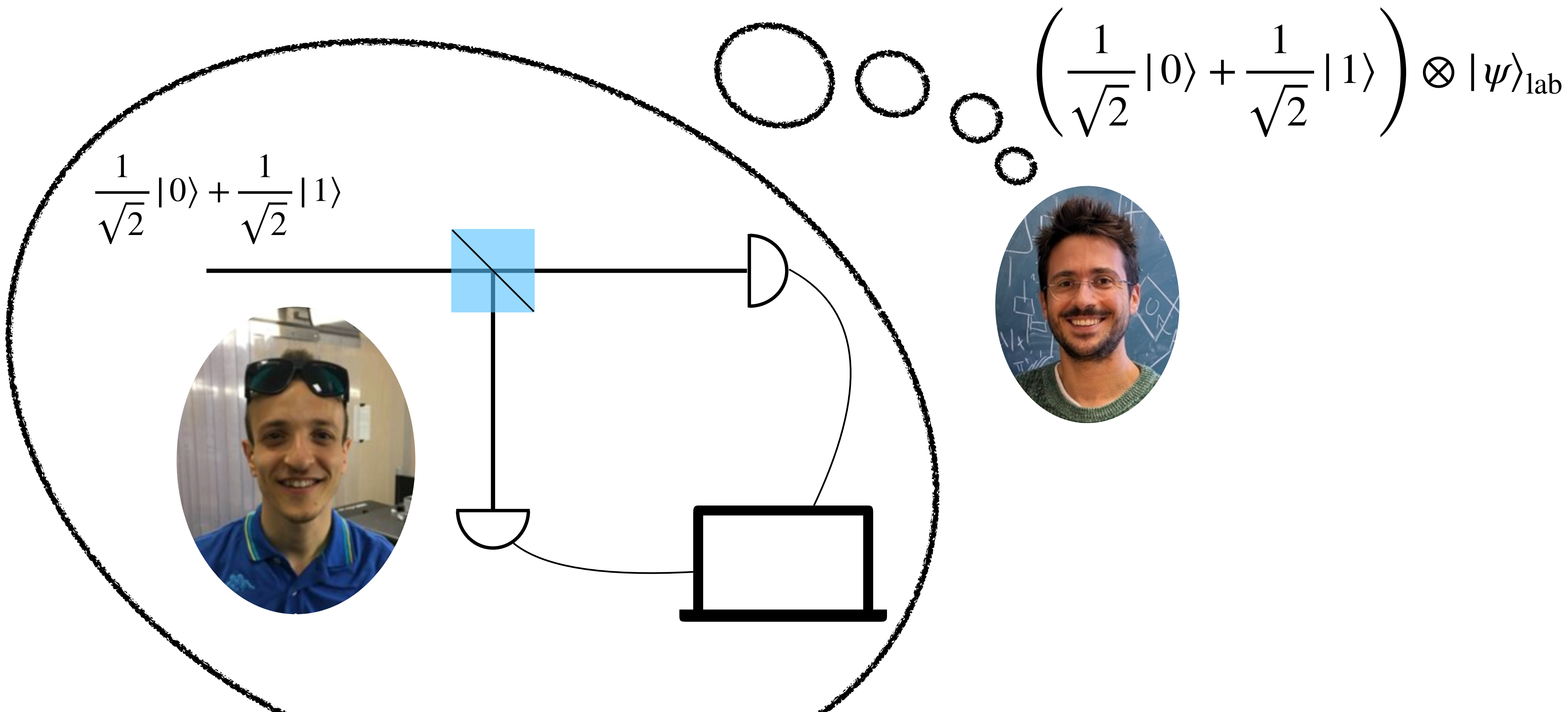
Bell, Wigner

friends



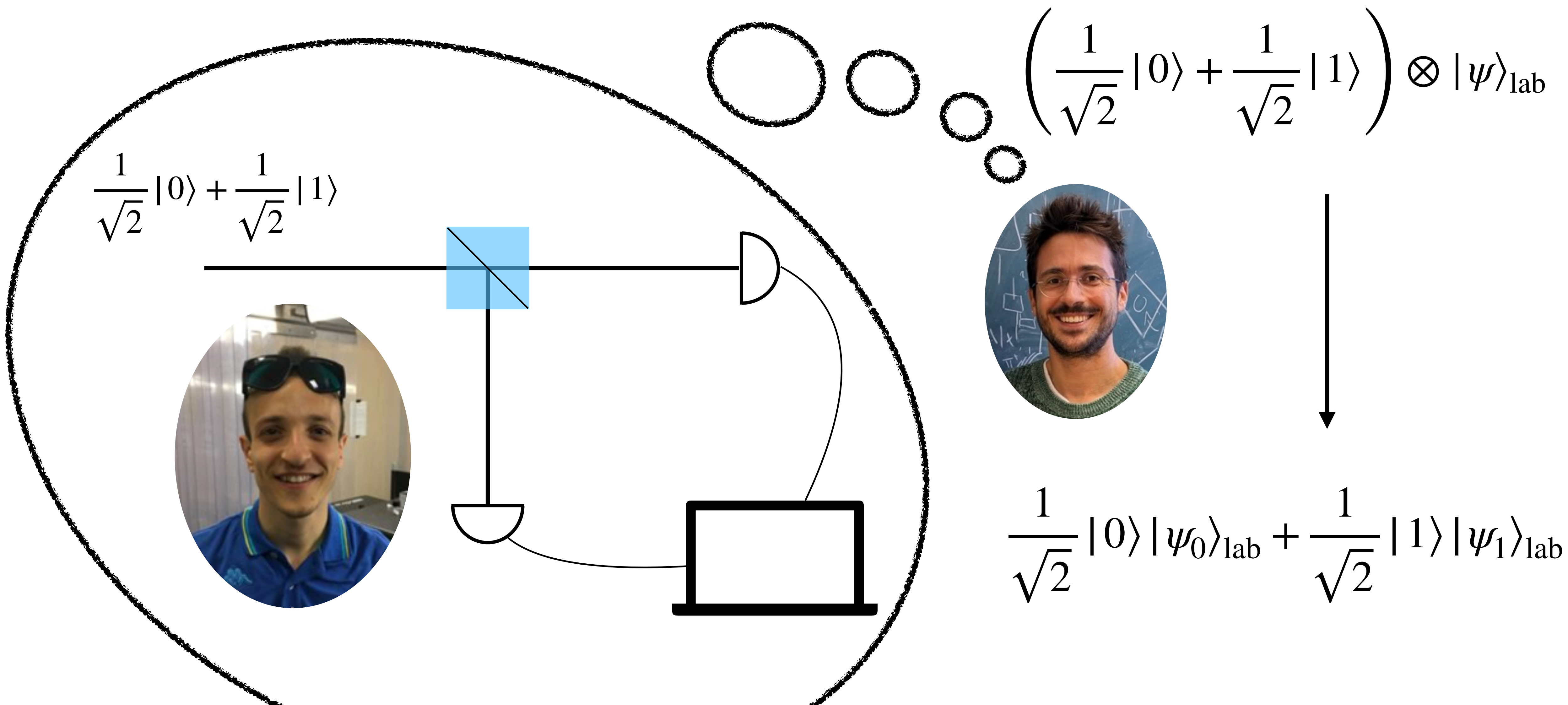
Bell, Wigner

friends



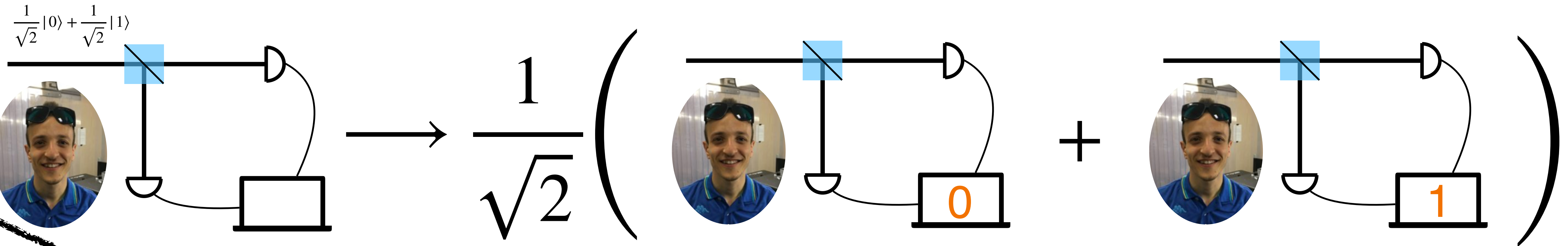
Bell, Wigner

friends



Bell, Wigner

friends



Wigner's friend

is Emanuele really in a superposition?

whenever I look in the lab, I see him in a definite state

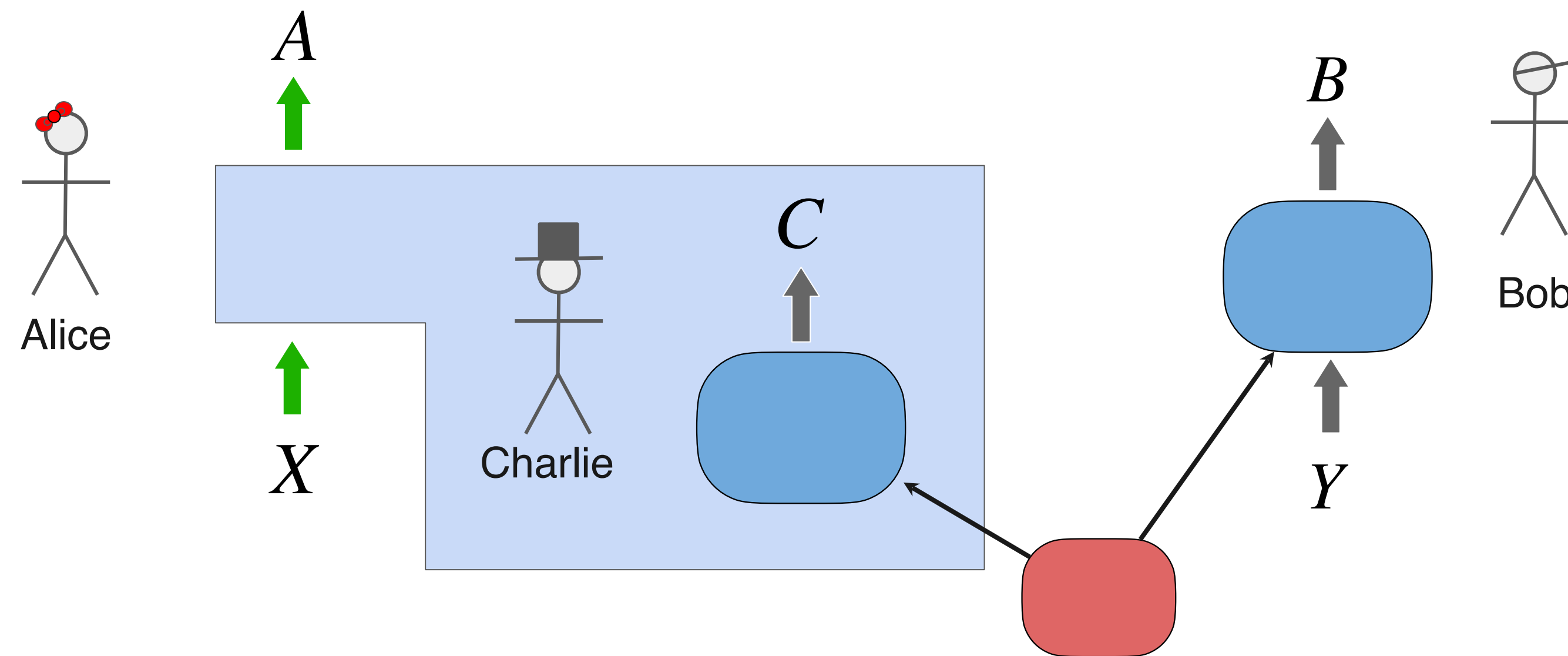
it *must* just be a matter of lacking information, not a real superposition... right?

a problem with the quantum description

similar situation as with EPR... quantum theory said the outcomes were random, but there was a local hidden variable model for the the EPR correlations



extended Wigner's friend scenario



violations of certain inequalities in conflict
with intuitive metaphysical assumptions

A No-Go Theorem for Observer-Independent Facts

by Časlav Brukner^{1,2} 

Entropy **2018**, *20*(5), 350; <https://doi.org/10.3390/e20050350>

extended Wigner's friend

other theorems

PAPER • OPEN ACCESS

A possibilistic no-go theorem on the Wigner's friend paradox

Marwan Haddara and Eric G Cavalcanti

[New Journal of Physics](#), [Volume 25](#), [September 2023](#)

arXiv:2209.03940 (quant-ph)

[Submitted on 8 Sep 2022]

A no-go theorem for absolute observed events without inequalities or modal logic

[Nick Ormrod](#), [Jonathan Barrett](#)

arXiv:2308.16220 (quant-ph)

[Submitted on 30 Aug 2023]

A review and analysis of six extended Wigner's friend arguments

[David Schmid](#), [Yìlè Yīng](#), [Matthew Leifer](#)



A “thoughtful” Local Friendliness no-go theorem: a prospective experiment with new assumptions to suit

Howard M. Wiseman^{1,2}, Eric G. Cavalcanti³, and Eleanor G. Rieffel⁴

Doi: <https://doi.org/10.22331/q-2023-09-14-1112>

Citation: Quantum 7, 1112 (2023).

QUANTUM MECHANICS

Facts are relative

[Časlav Brukner](#)

[Nature Physics](#) **16**, 1172–1174 (2020)

[Home](#) > [Foundations of Physics](#) > [Article](#)

When Greenberger, Horne and Zeilinger Meet Wigner’s Friend

[Open access](#) | Published: 27 June 2022

Volume 52, article number 68, (2022) [Cite this article](#)

[Gijs Leegwater](#)

Article | [Open access](#) | Published: 18 September 2018

Quantum theory cannot consistently describe the use of itself

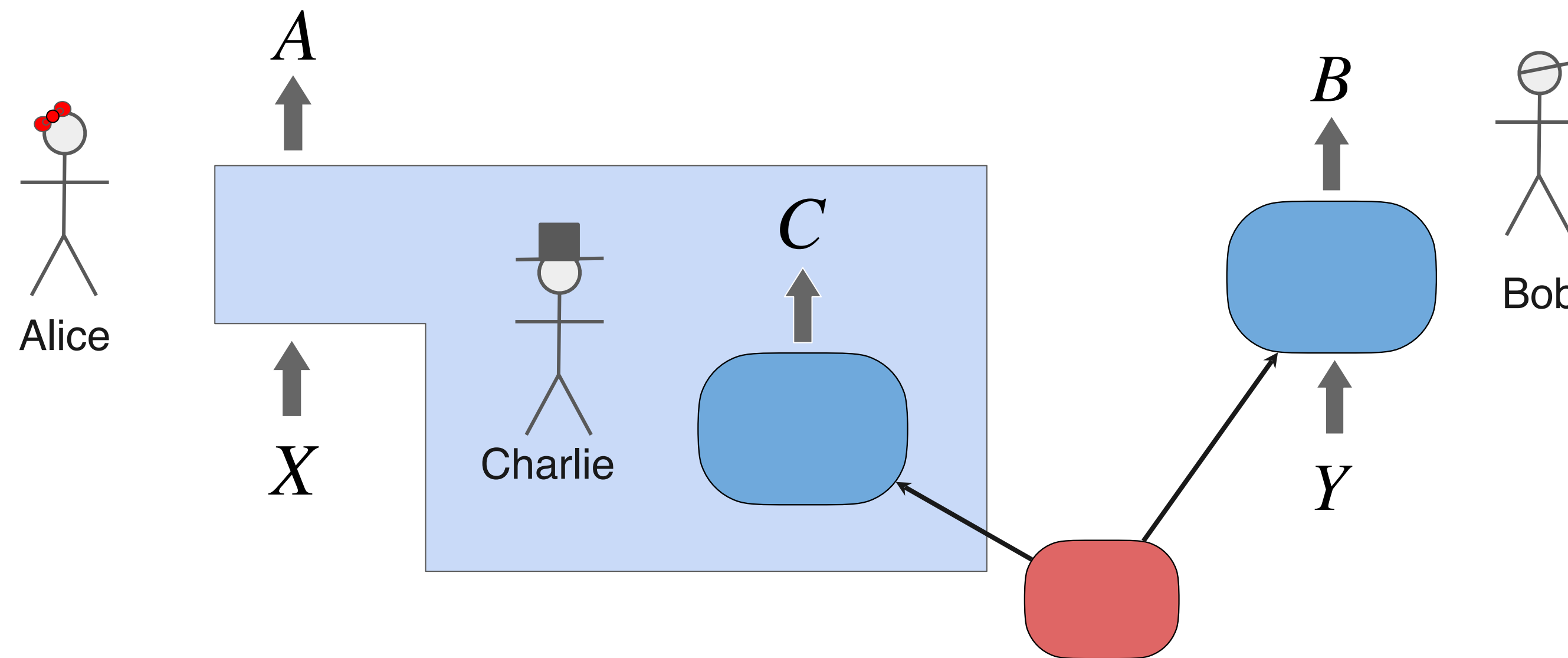
[Daniela Frauchiger](#) & [Renato Renner](#)

[Nature Communications](#) **9**, Article number: 3711 (2018)

plan

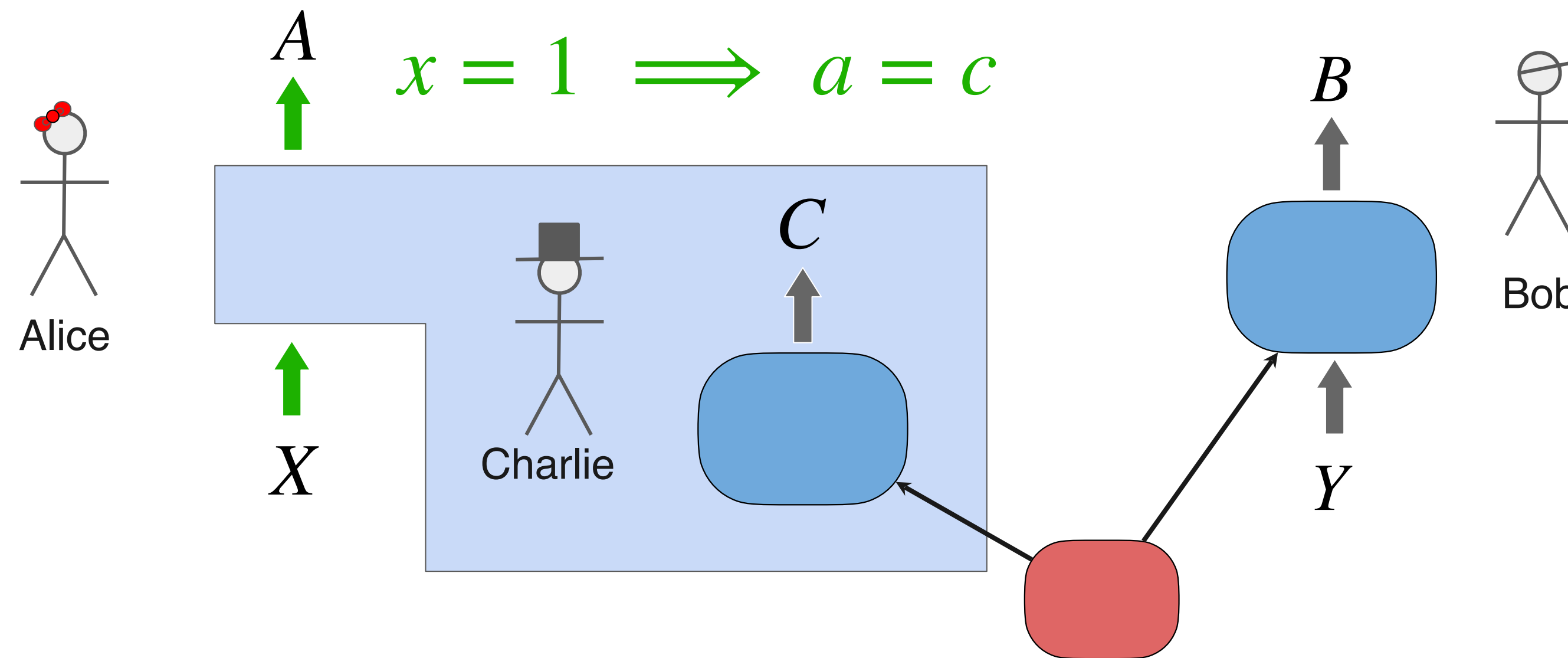
- **local friendliness theorem**
- **constraints on interpretations: relation to Bell**
- **causal modelling**
 - **classical causal modelling cannot explain Bell inequality violations**
 - **solution: (post) quantum causal modelling**
 - **causal modelling cannot explain LF inequality violations**

extended Wigner's friend scenario



$$f(ab | xy)$$

extended Wigner's friend scenario



$$f(ab | xy)$$

$$f(abc | x = 1, y)$$

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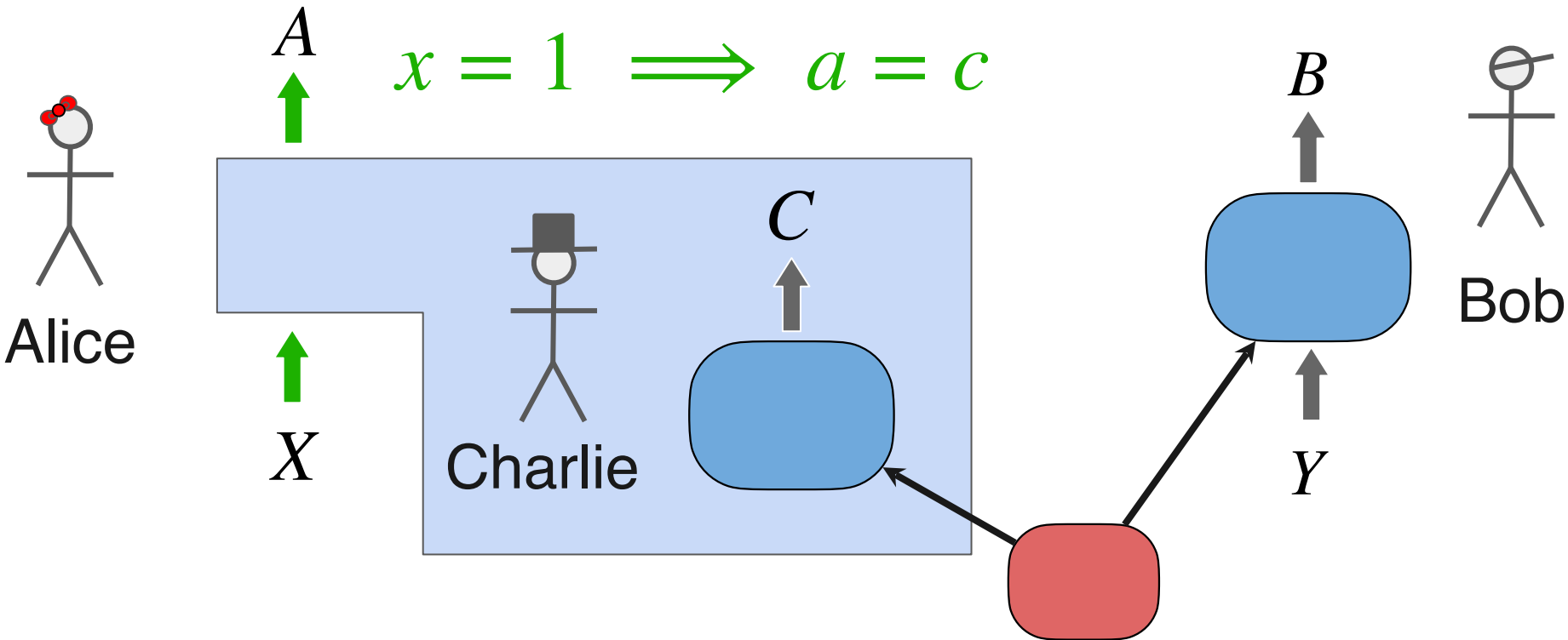
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LF no-go theorem



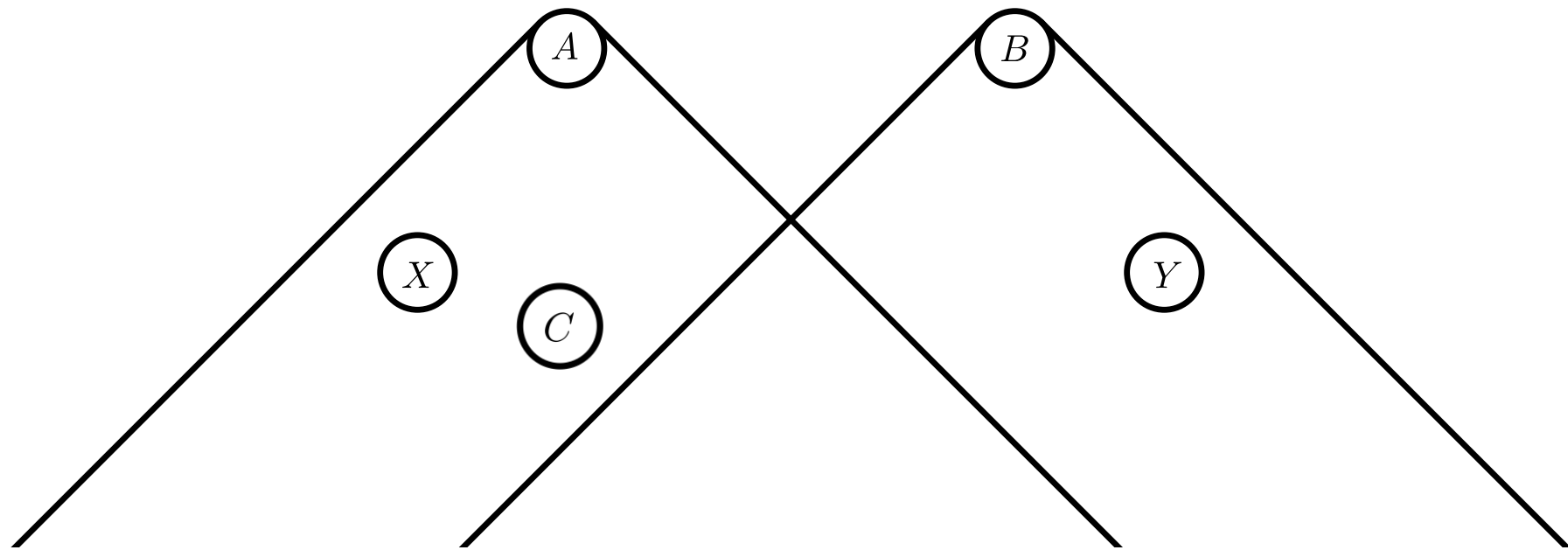
$$f(ab | xy)$$

$$f(ab | xy) = \sum_c p(abc | xy)$$

$$p(a = c | x = 1) = 1$$

$$p(c | xy) = p(c)$$

$$p(a | cxy) = p(a | cx)$$
$$p(b | cxy) = p(b | y)$$



absoluteness of
observed events

no
superdeterminism

locality

LF inequalities

incompatible with QM!
**if observers can be treated as
quantum systems**

Article | [Published: 17 August 2020](#)

A strong no-go theorem on the Wigner's friend paradox

[Kok-Wei Bong](#), [Aníbal Utreras-Alarcón](#), [Farzad Ghafari](#), [Yeong-Cherng Liang](#), [Nora Tischler](#) , [Eric G. Cavalcanti](#) , [Geoff J. Pryde](#) & [Howard M. Wiseman](#)

[Nature Physics](#) **16**, 1199–1205 (2020) | [Cite this article](#)

closing remarks

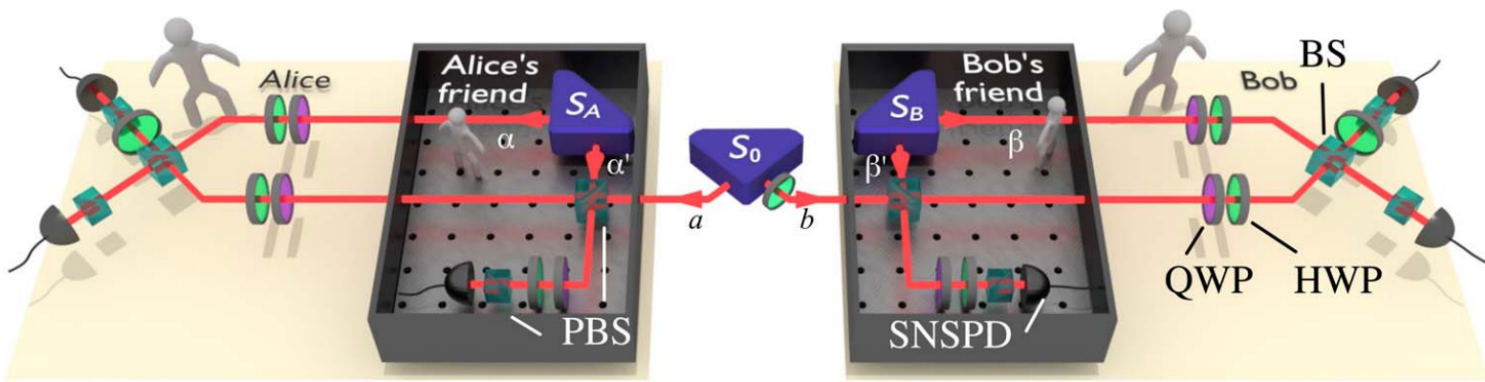
experimental realisations

SCIENCE ADVANCES | RESEARCH ARTICLE

PHYSICS

Experimental test of local observer independence

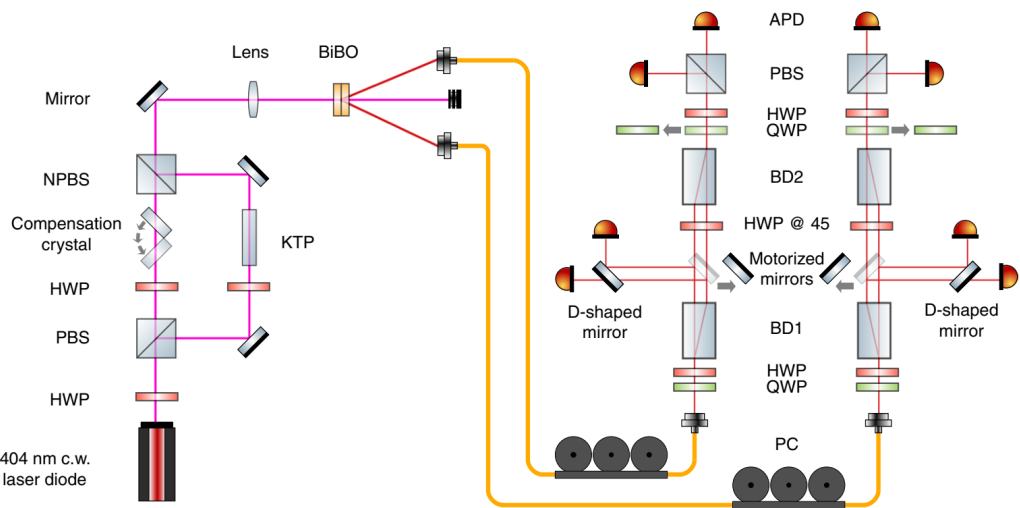
Massimiliano Proietti¹, Alexander Pickston¹, Francesco Graffitti¹, Peter Barrow¹, Dmytro Kundys¹, Cyril Branciard², Martin Ringbauer^{1,3}, Alessandro Fedrizzi^{1*}



ARTICLES
<https://doi.org/10.1038/s41567-020-0990-x>

A strong no-go theorem on the Wigner's friend paradox

Kok-Wei Bong^{1,4}, Aníbal Utreras-Alarcón^{1,4}, Farzad Ghafari¹, Yeong-Cherng Liang², Nora Tischler¹, Eric G. Cavalcanti³, Geoff J. Pryde¹ and Howard M. Wiseman¹

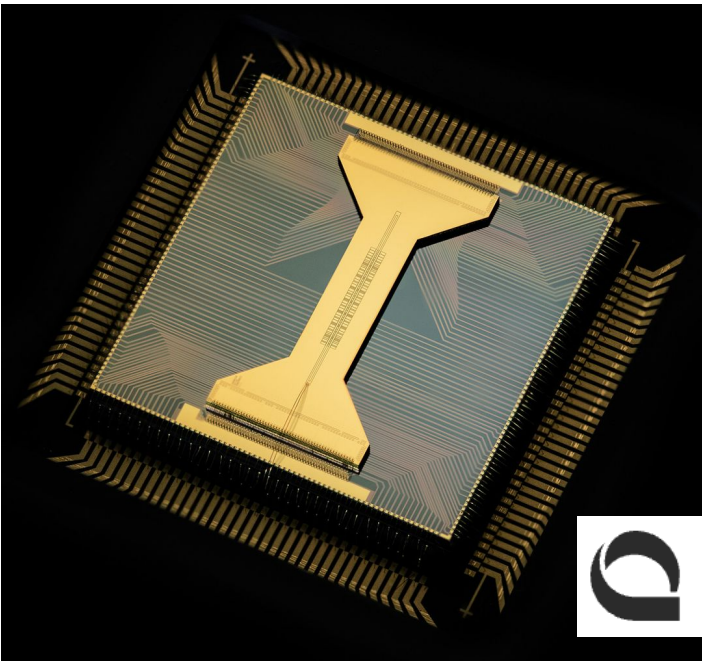


arXiv:2409.15302 (quant-ph)

[Submitted on 4 Sep 2024 (v1), last revised 3 Jun 2025 (this version, v2)]

Towards violations of Local Friendliness with quantum computers

William J. Zeng, Farrokh Labib, Vincent Russo



16 qubits



photonic qubit

16 qubits

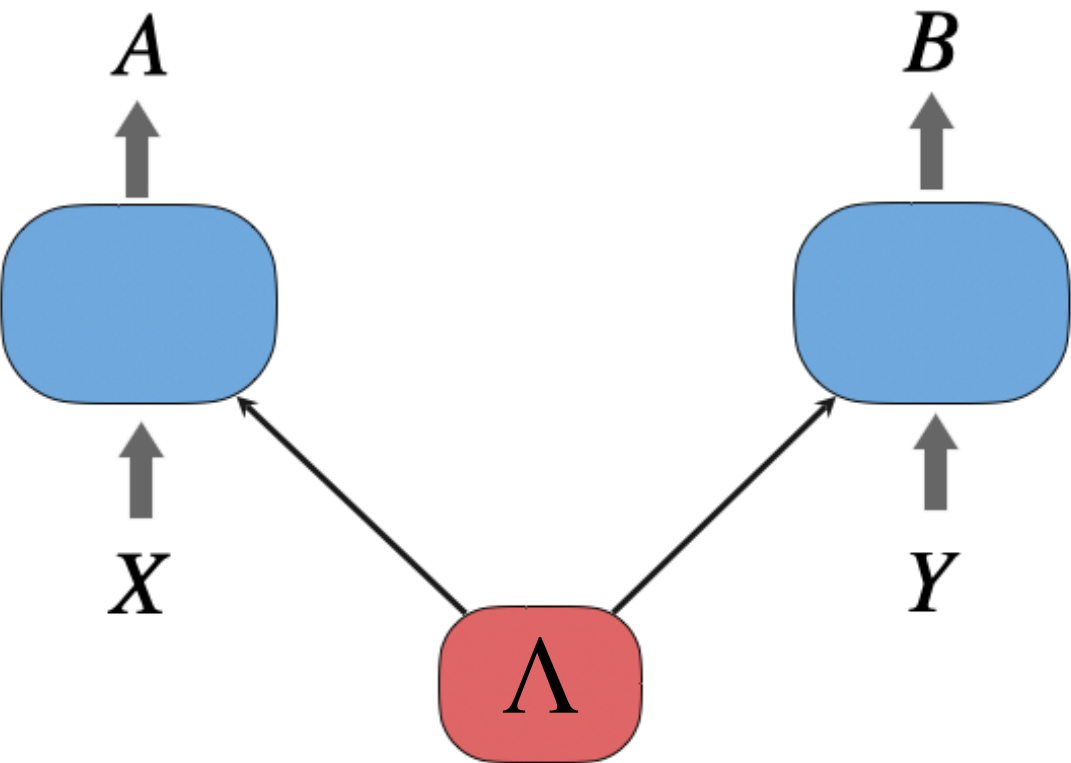
human level AI human animal

cat

increasingly credible friend

metaphysics roadmap

Bell's theorem



$$f(ab | xy) = \sum_{\lambda} p(ab | xy\lambda)p(\lambda | xy)$$

$$p(a | \lambda xy) = p(a | \lambda x)$$
$$p(b | \lambda xy) = p(b | \lambda y)$$

$$p(ab | xy\lambda) \in \{0,1\}$$

locality

pre-determination

Bell inequalities

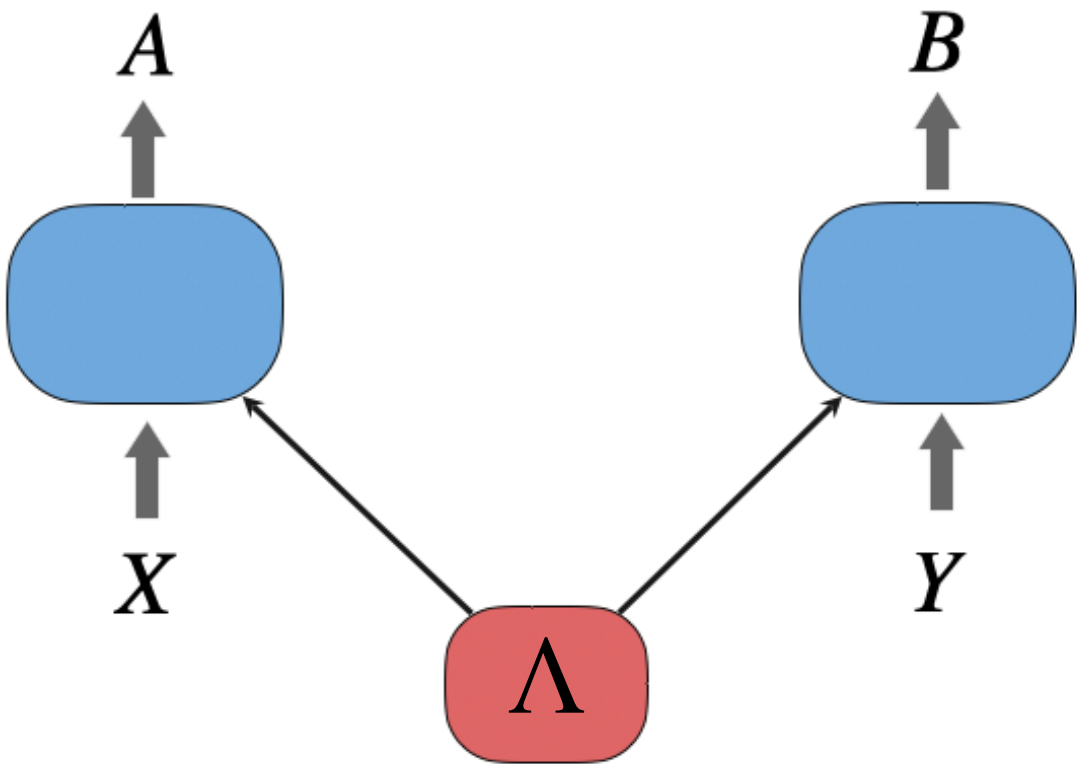
no
superdeterminism

↖ Bell 1964

$$p(\lambda | xy) = p(\lambda)$$

[1] Wiseman and Cavalcanti (2015) Causarum Investigatio and the Two Bell's Theorems of John Bell, Quantum [Un]speakables II
[2] Cavalcanti and Wiseman (2021) Implications of Local Friendliness violations for quantum causality, Entropy 23, 8

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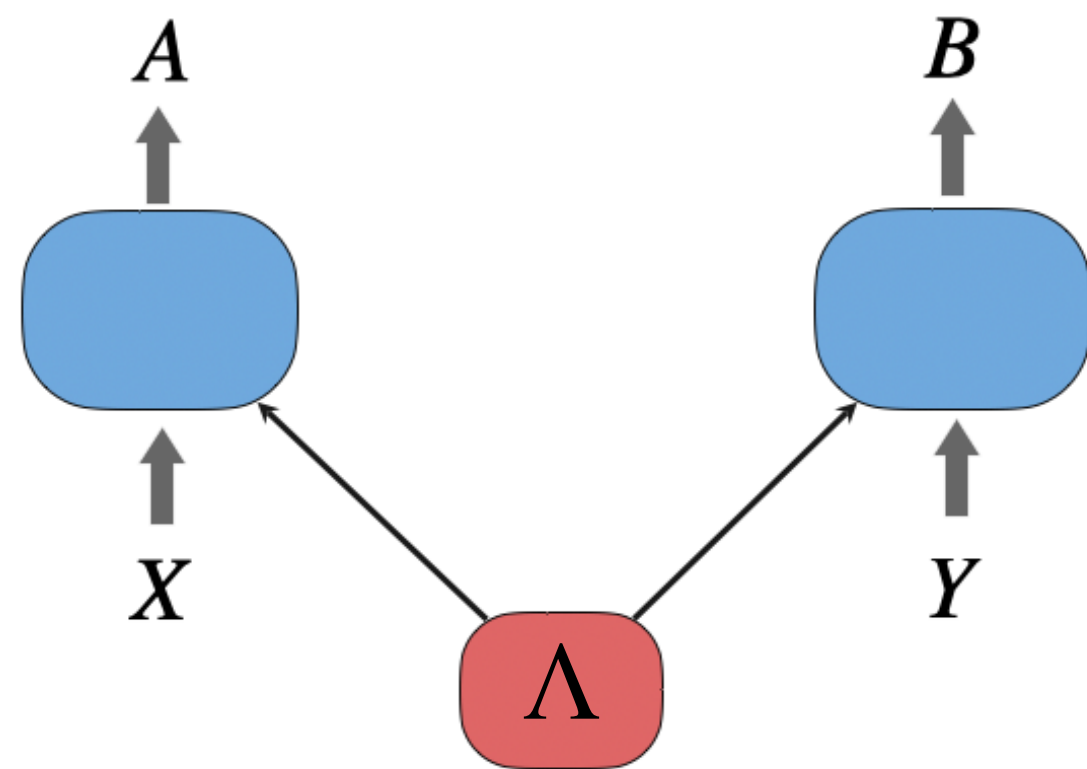
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locality

pre-determination

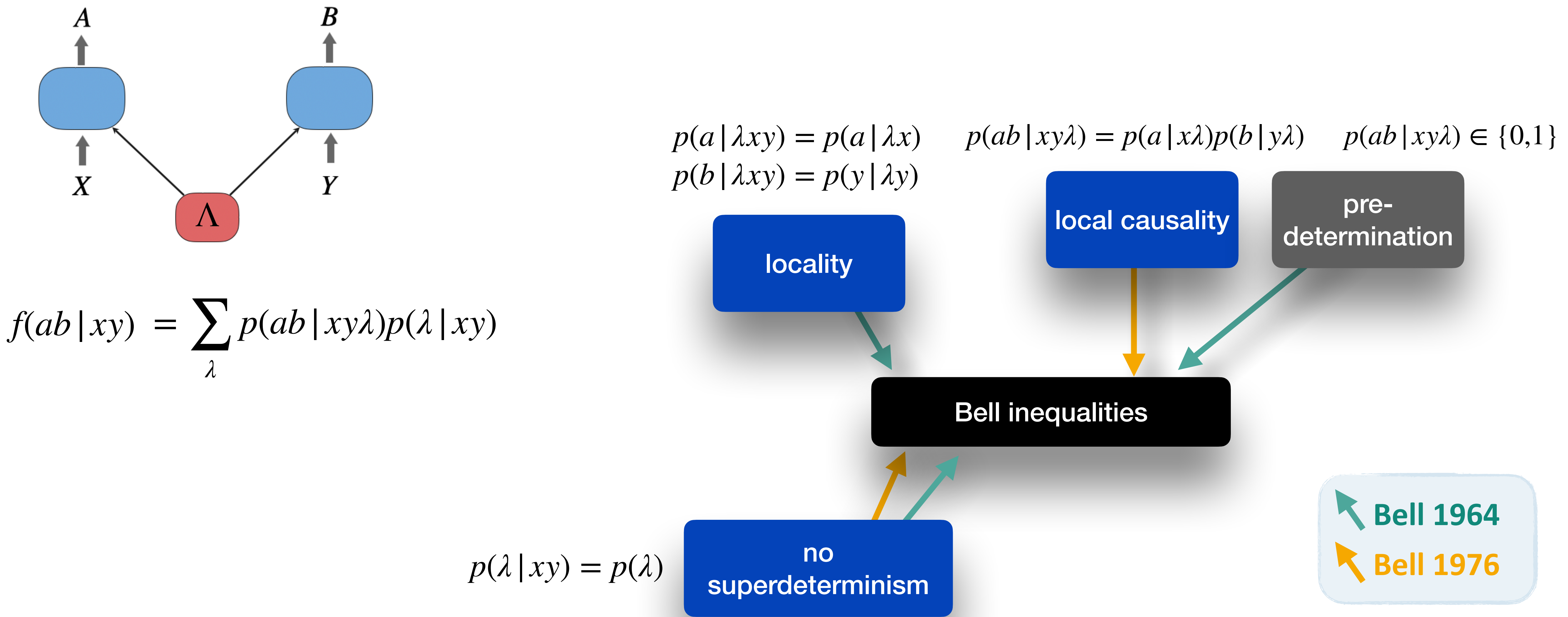
Bell inequalities

no
superdeterminism

↖ Bell 1964

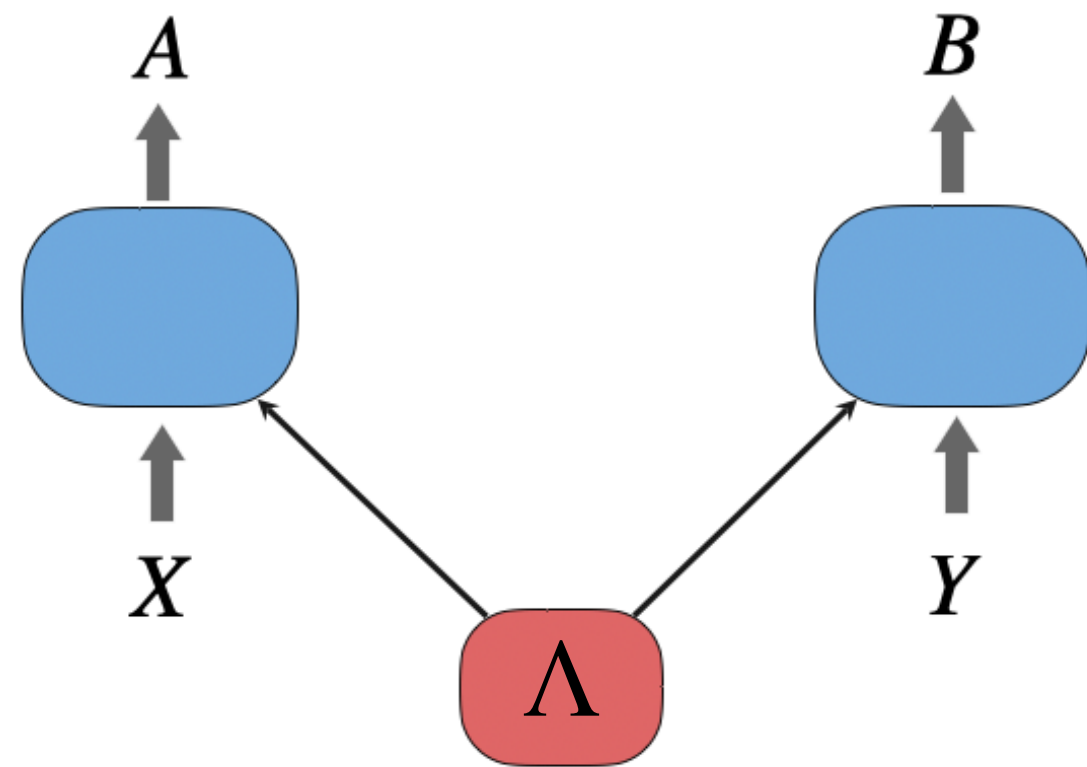
$$p(\lambda | xy) = p(\lambda)$$

Bell's second theorem

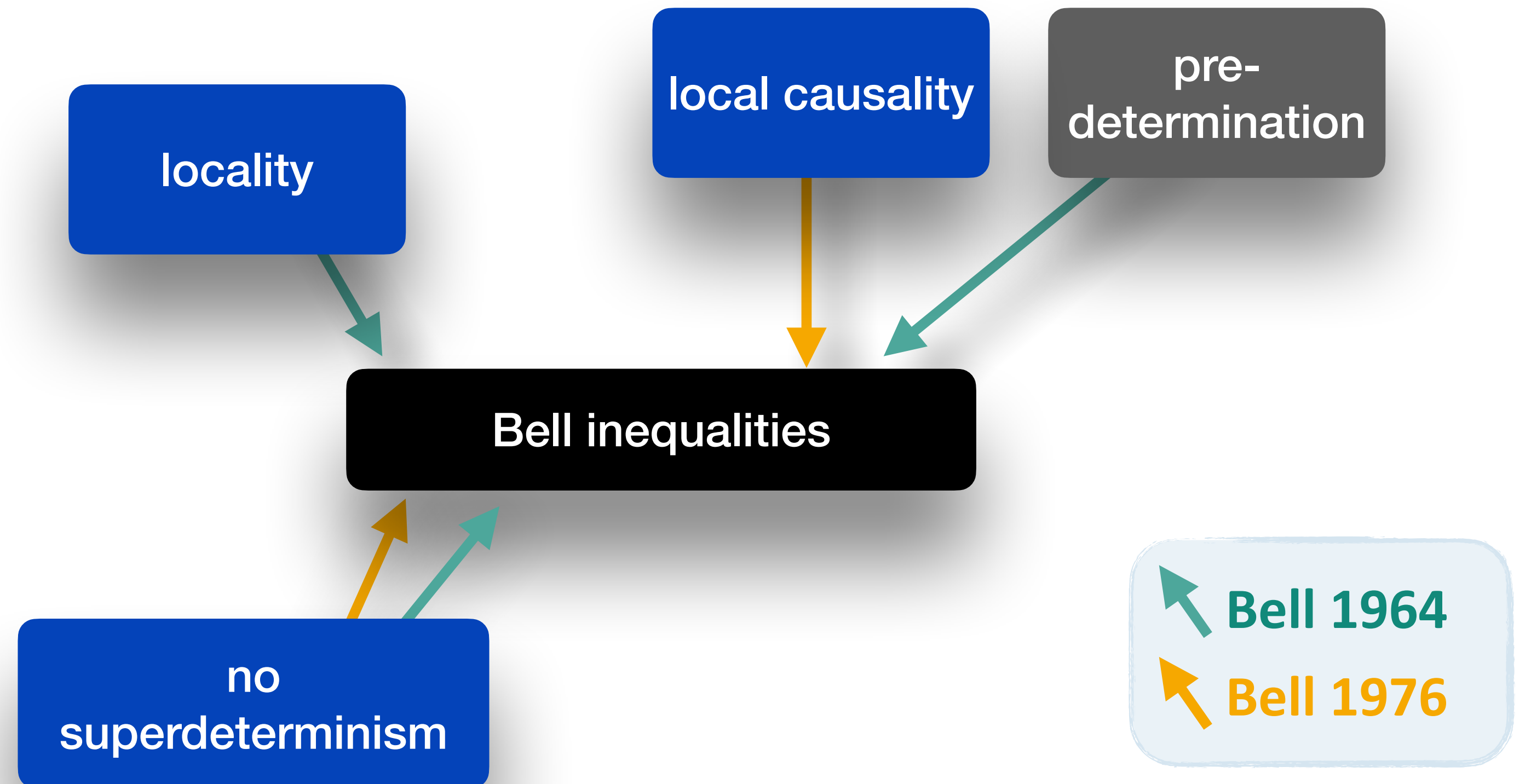


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Bell's second theorem



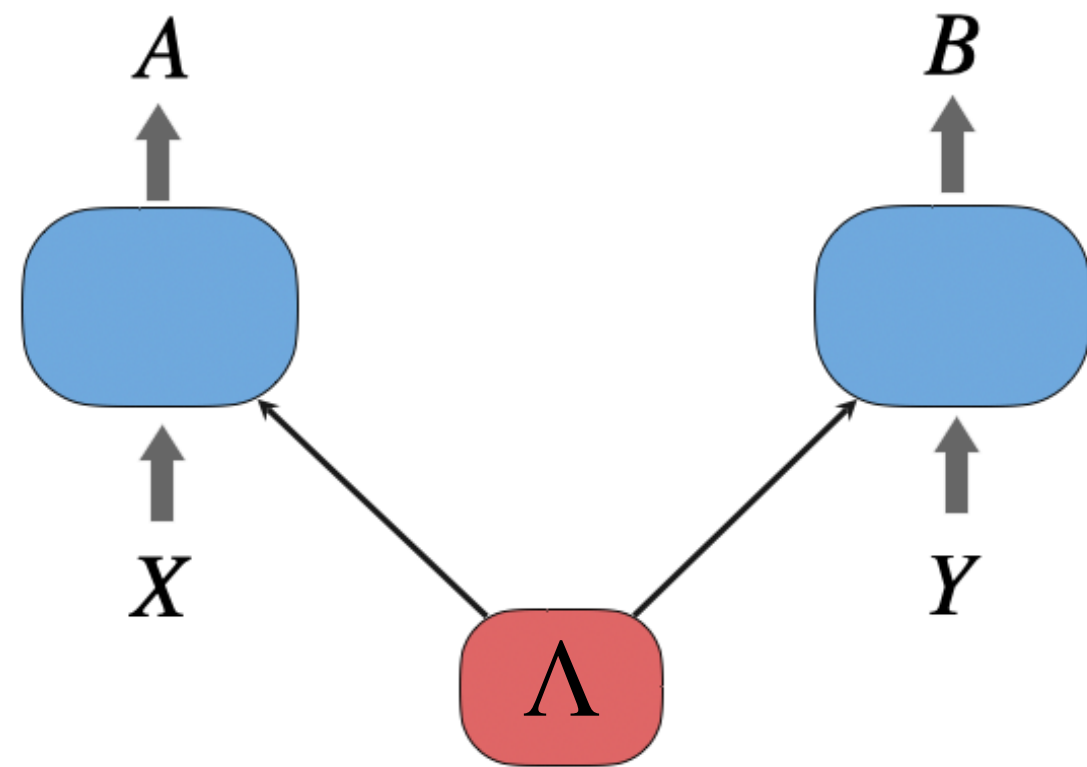
$$f(ab | xy) = \sum_{\lambda} p(ab | xy\lambda)p(\lambda | xy)$$



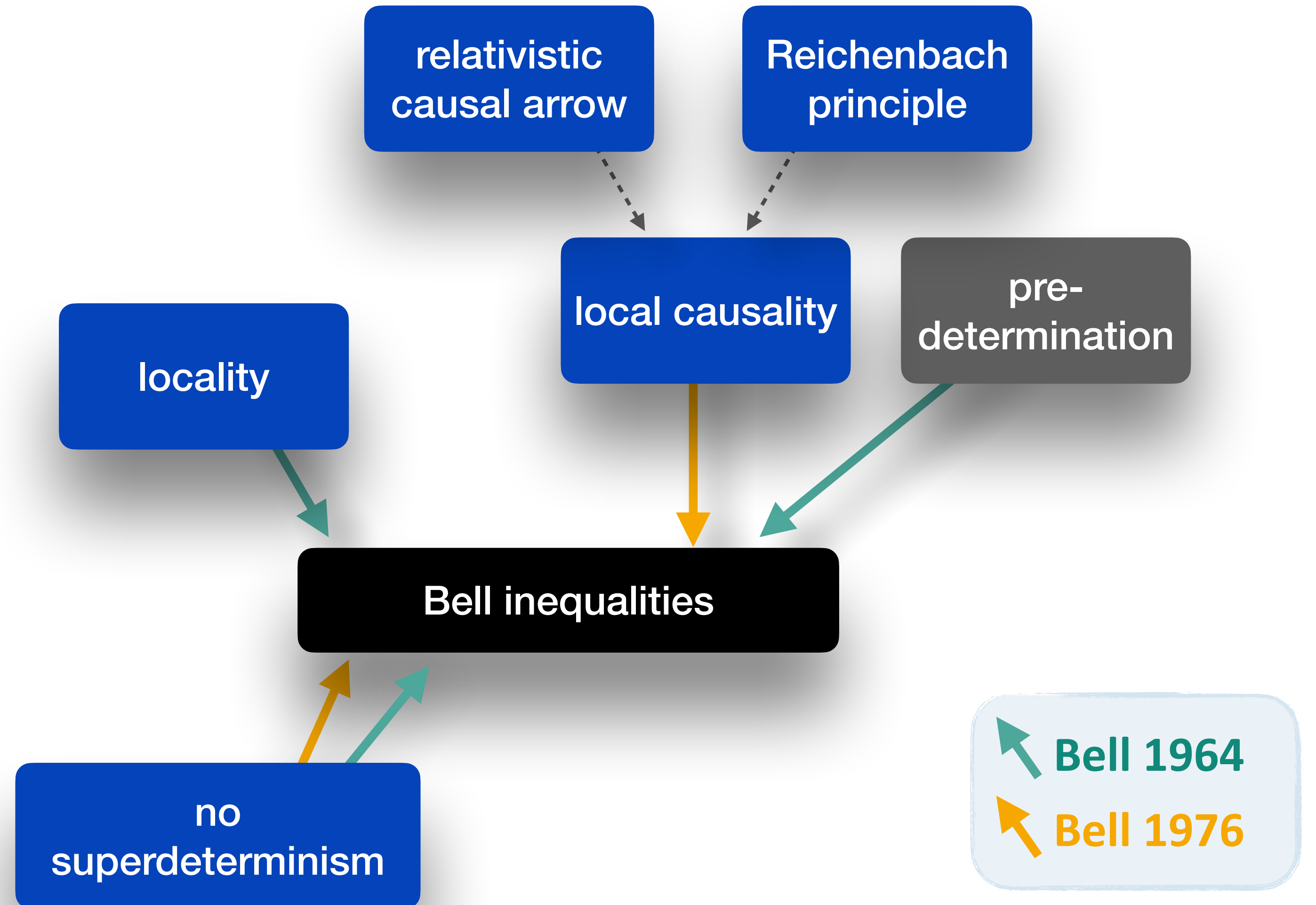
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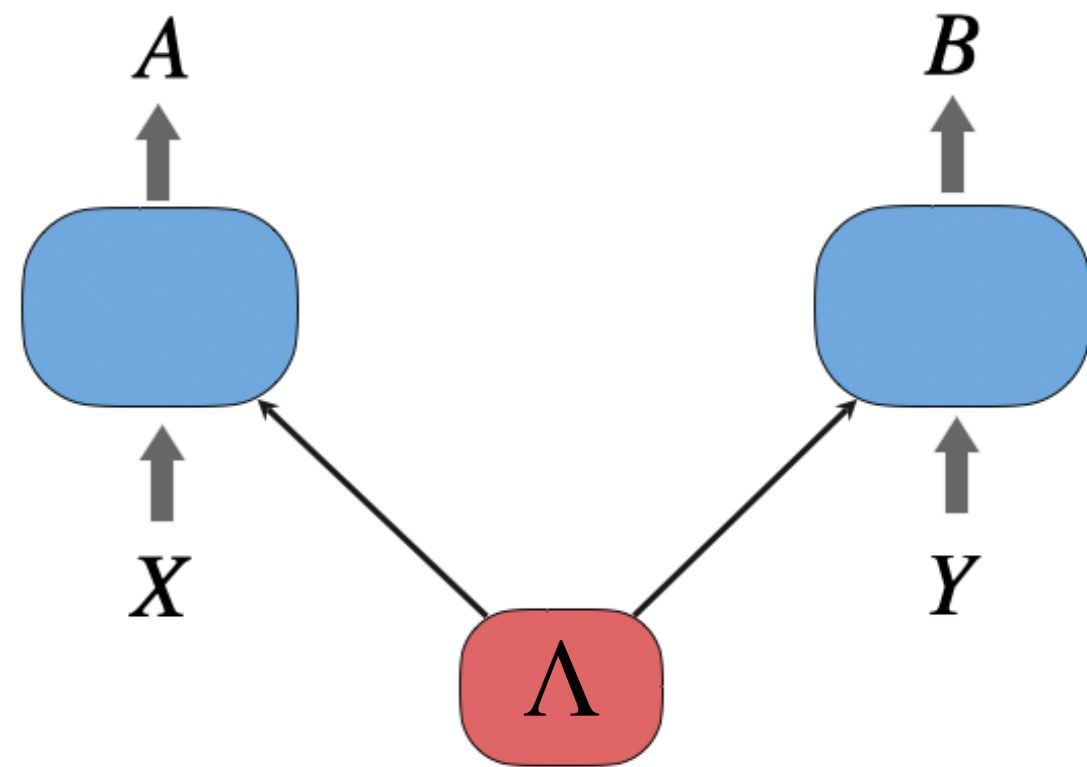
Bell's second theorem



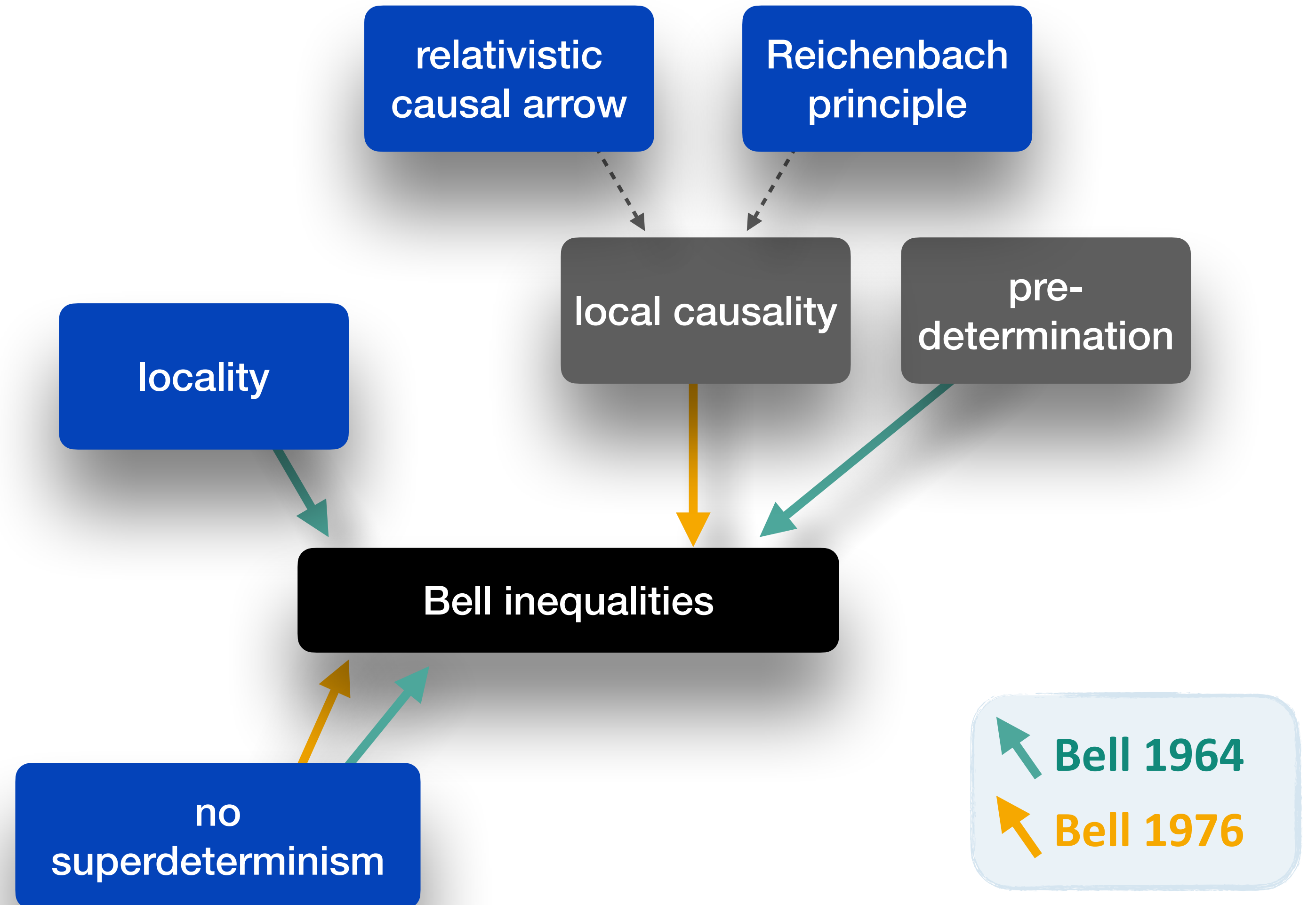
$$f(ab | xy) = \sum_{\lambda} p(ab | xy\lambda)p(\lambda | xy)$$



Bell's second theorem



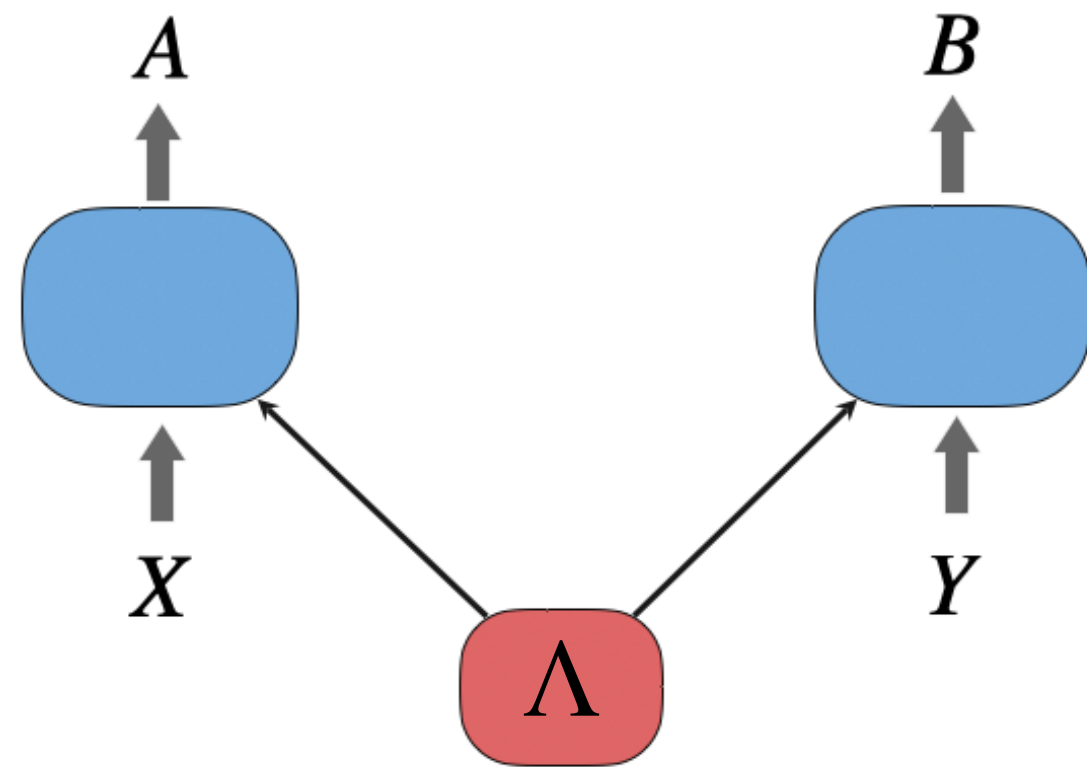
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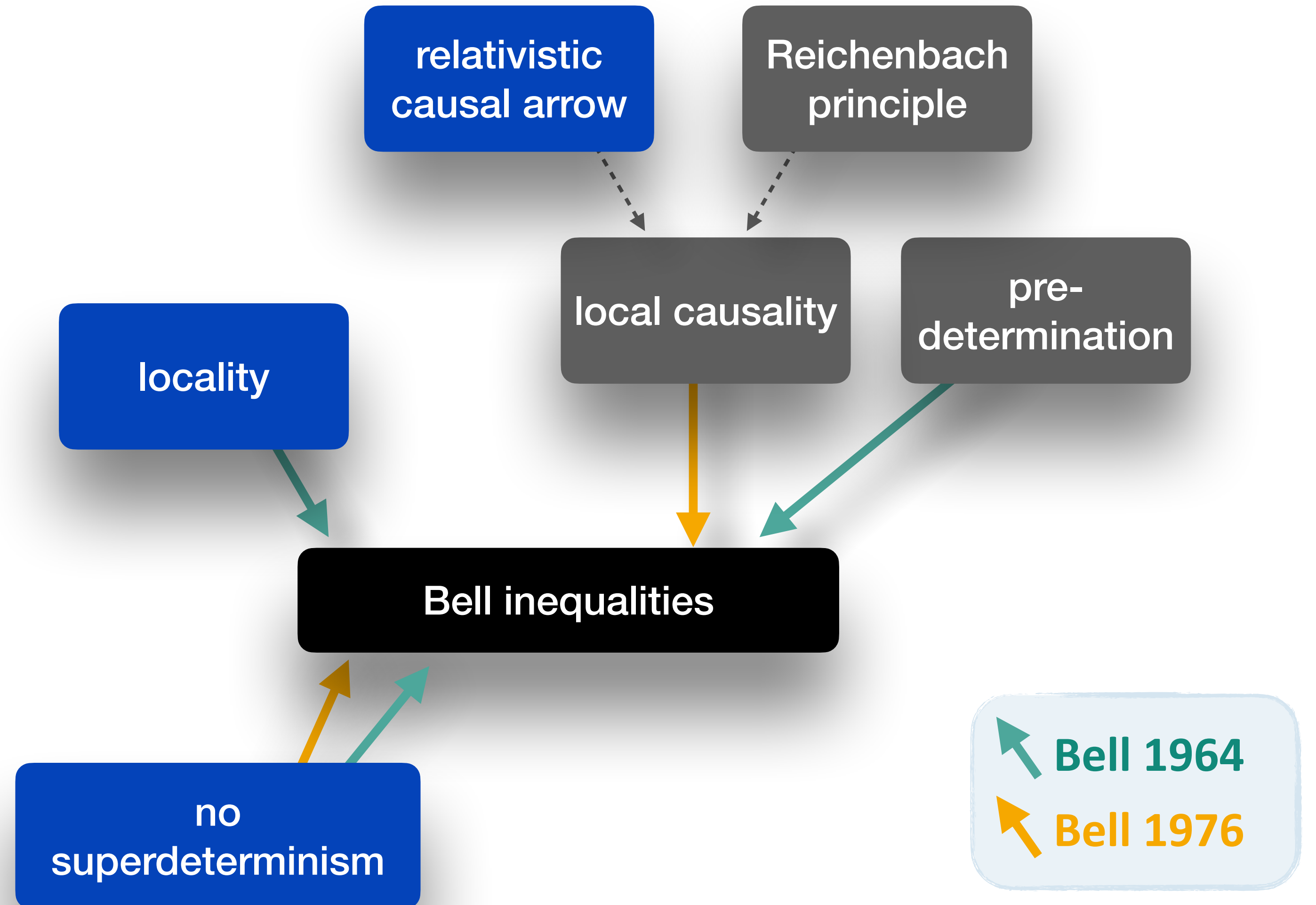
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Bell's second theorem



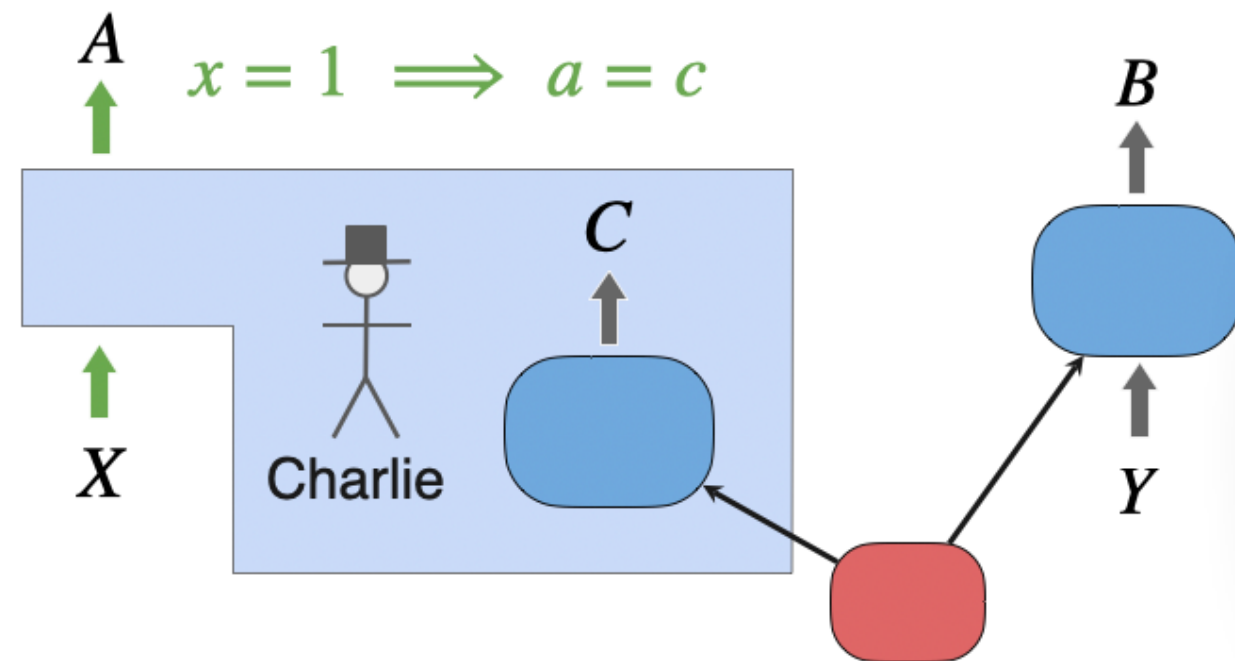
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[2] Cavalcanti and Wiseman (2021) Implications of Local Friendliness violations for quantum causality, Entropy 23, 8

local-friendliness theorem



absoluteness of
observed events

relativistic
causal arrow

Reichenbach
principle

local causality

pre-
determination

locality

Bell inequalities

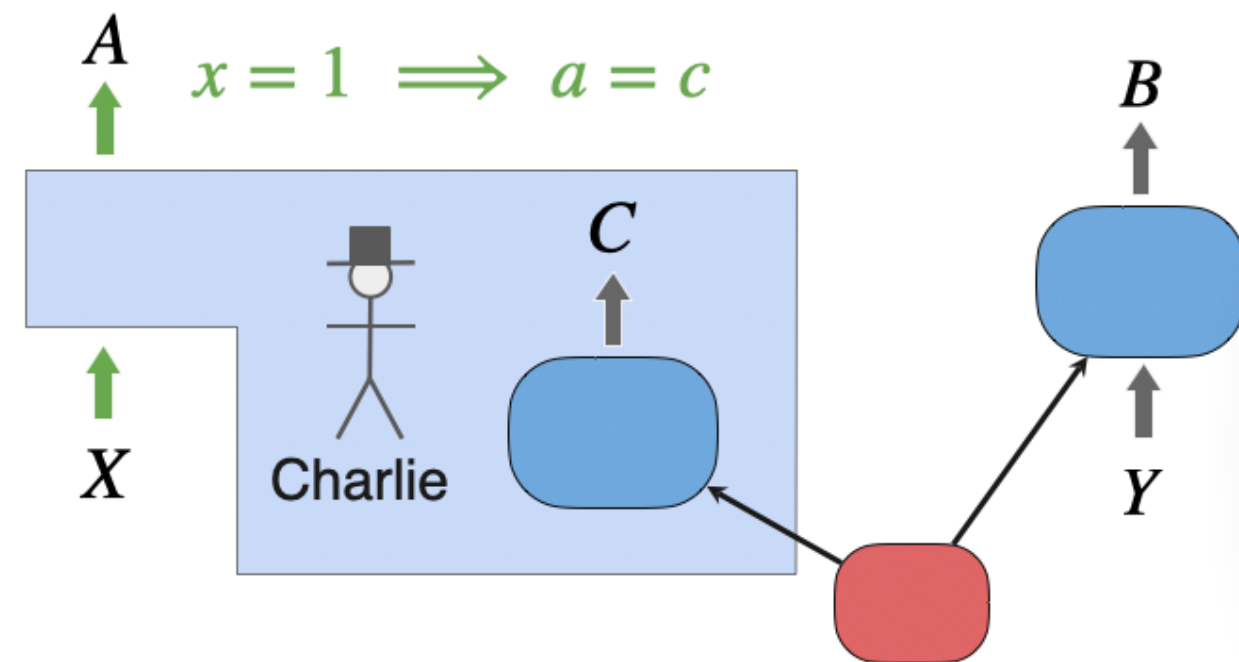
no
superdeterminism

↖ Bell 1964
↖ Bell 1976

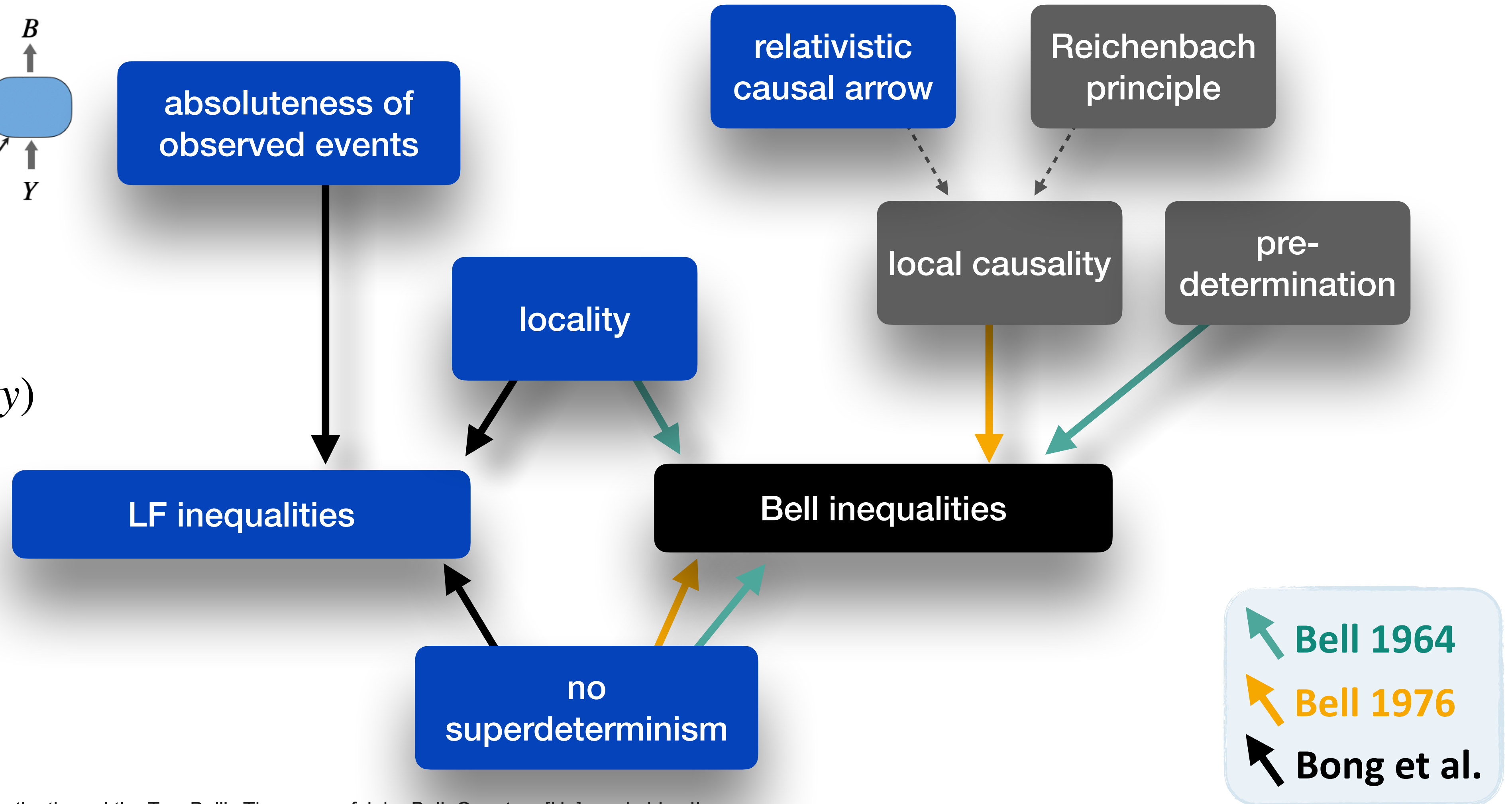
$$f(ab | xy) = \sum_c p(abc | xy)$$

[1] Wiseman and Cavalcanti (2015) Causarum Investigatio and the Two Bell's Theorems of John Bell, Quantum [Un]speakables II
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local-friendliness theorem



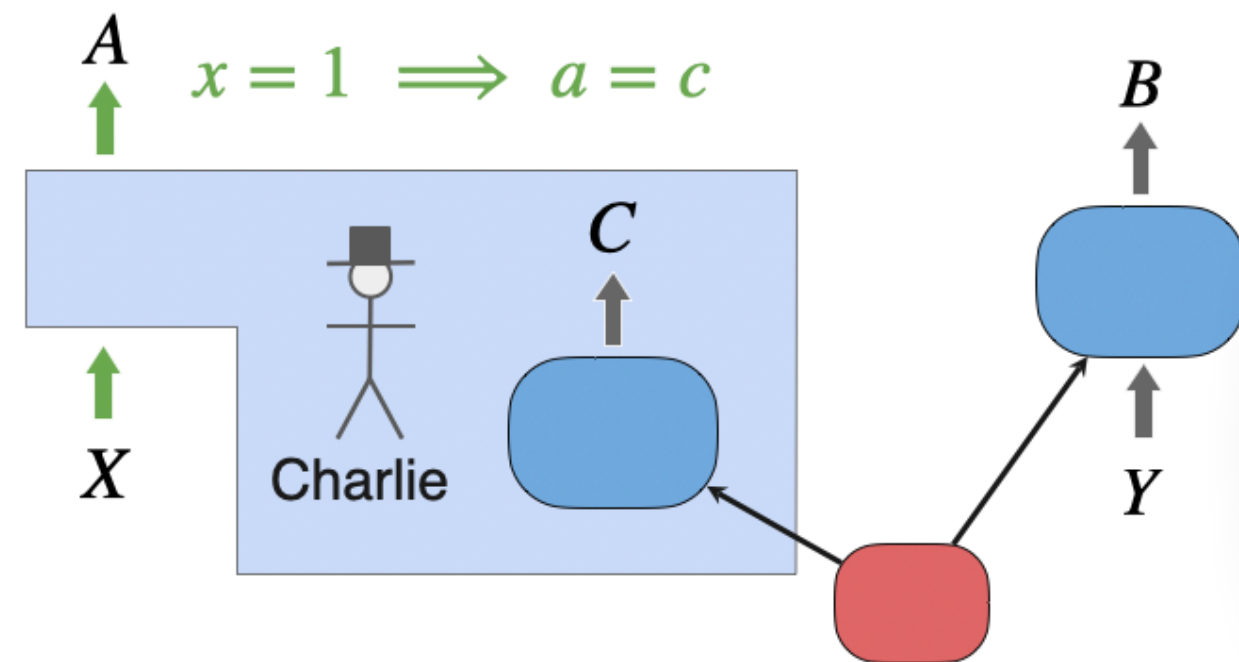
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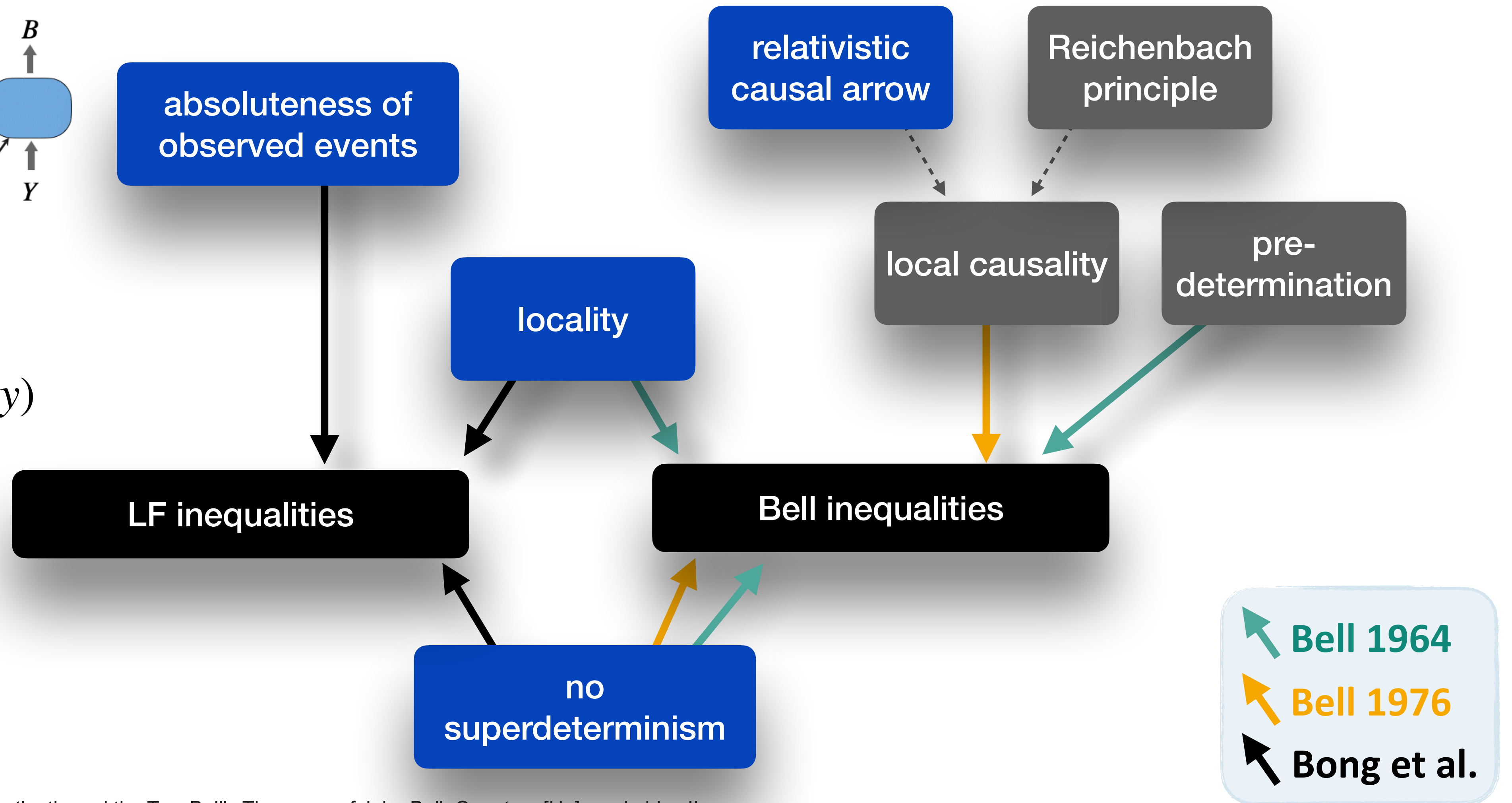
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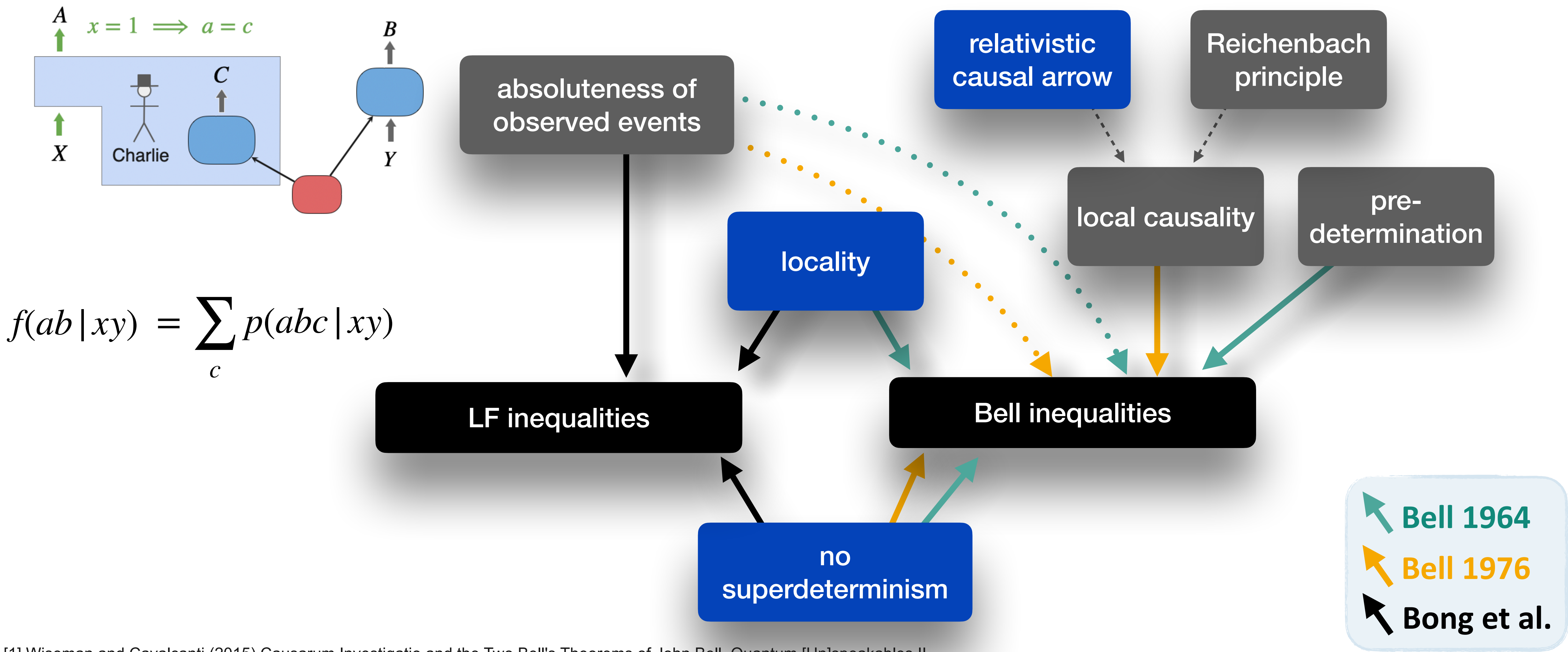
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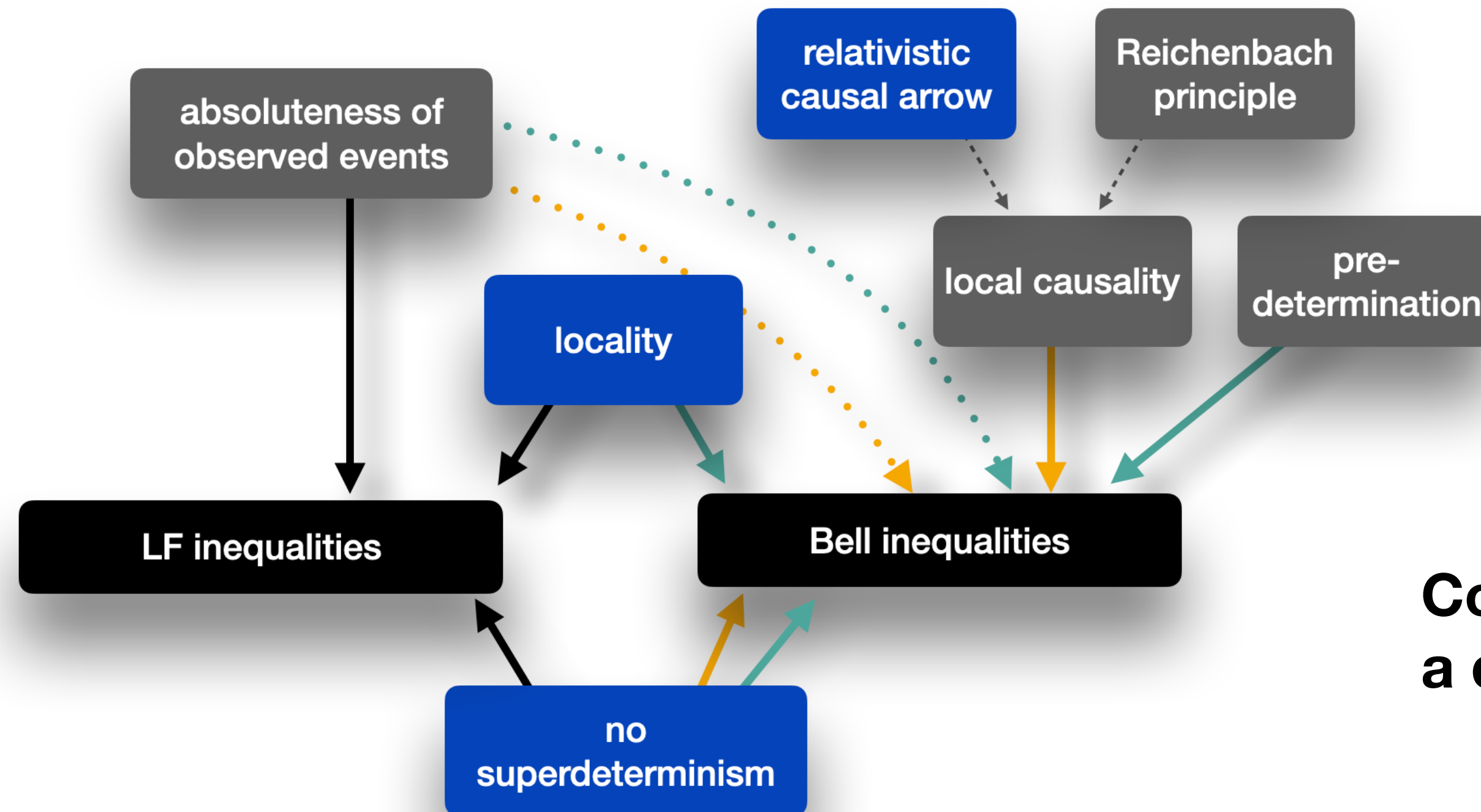
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[2] Cavalcanti and Wiseman (2021) Implications of Local Friendliness violations for quantum causality, Entropy 23, 8

implications for interpretations



interpretations resolving all theorems by dropping the same assumption:

- pilot wave theory (aka Bohmian mechanics)
- superdeterministic models
- Everettian QM (aka many worlds)

Copenhagen(ish) interpretations forced to drop a different assumption in each theorem

"no-interpretation" interpretation not good anymore
⇒ need to talk about what happens to different observers

alternatively, modify QM: spontaneous collapse, observers / consciousness fundamental

remarks

- EWF stands to WF like Bell stands to EPR
- observations of friend play the role of the hidden variables of Bell
- violations of LF inequalities already happened, but for small systems
- what is a good friend? ---> theory of observation
- letting go of absoluteness of observed events:
 - what does it mean? how does it happen?
 - assumption in Bell, revise?

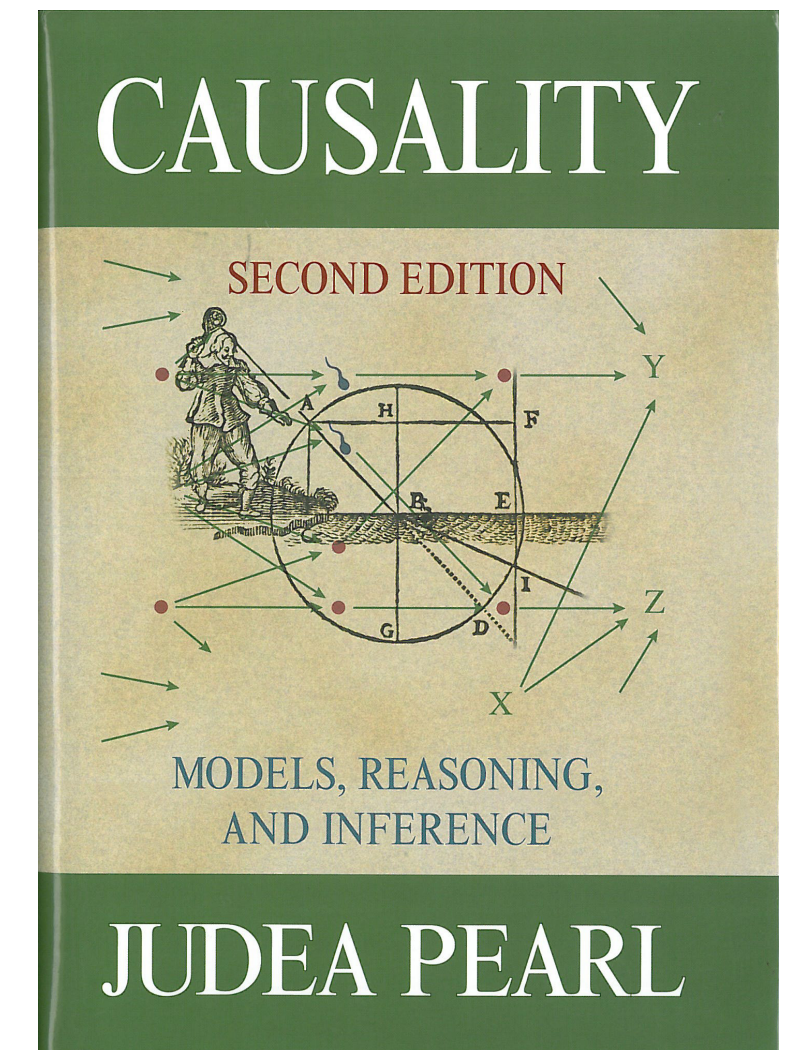
$$f(ab | xy) = \sum_c p(abc | xy)$$

$$p(a = c | x = 1) = 1$$

Bell and classical causal models

classical causal modelling

causal explanation
causal structure
+
compatible probability distribution

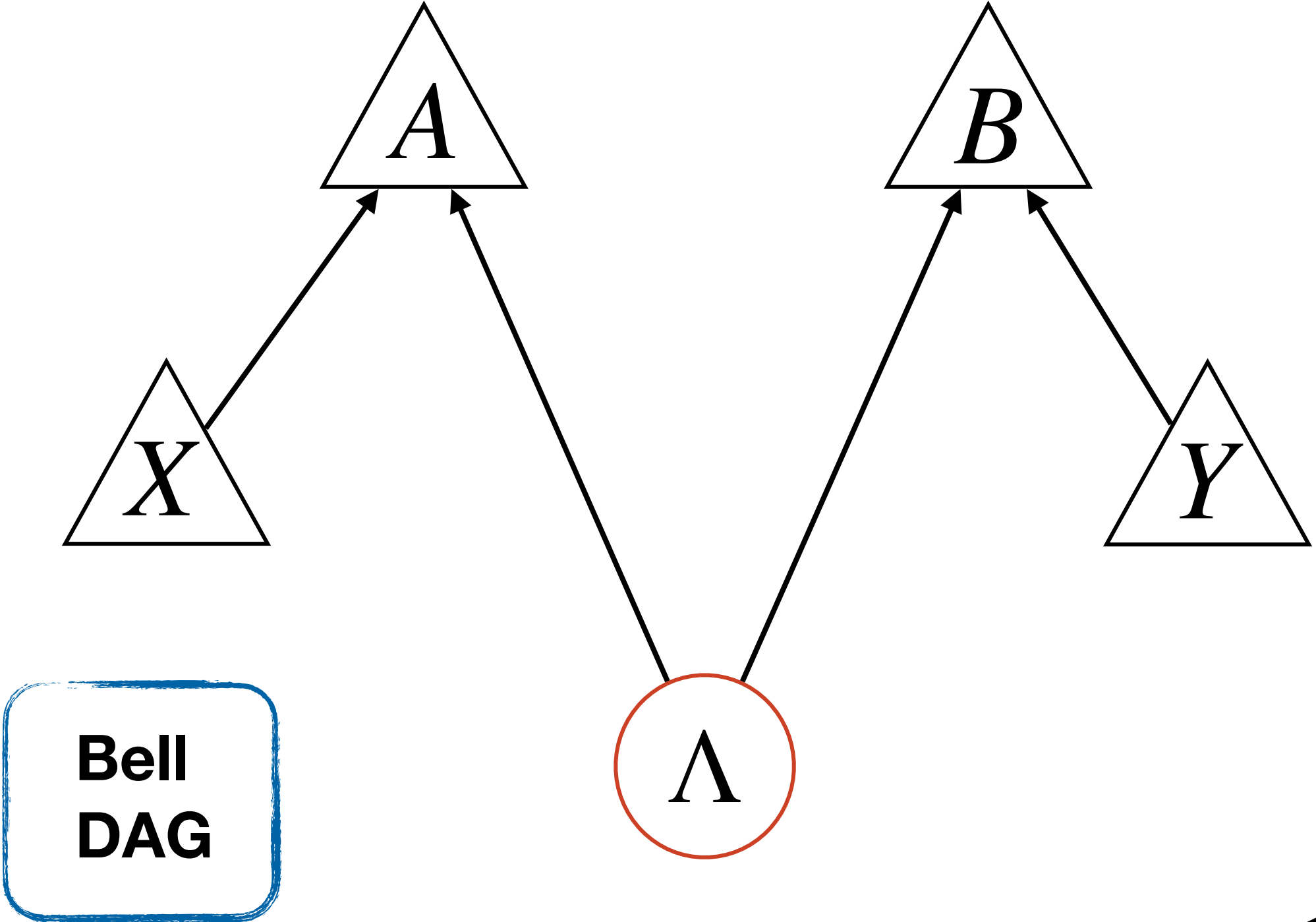


causal structure = a directed acyclic graph (DAG) (cause and effect relations)

compatibility = Markov conditions $\approx$ variables depend only on direct causes

used in medicine, economics, epidemiology, sociology, AI, etc...

Bell DAG



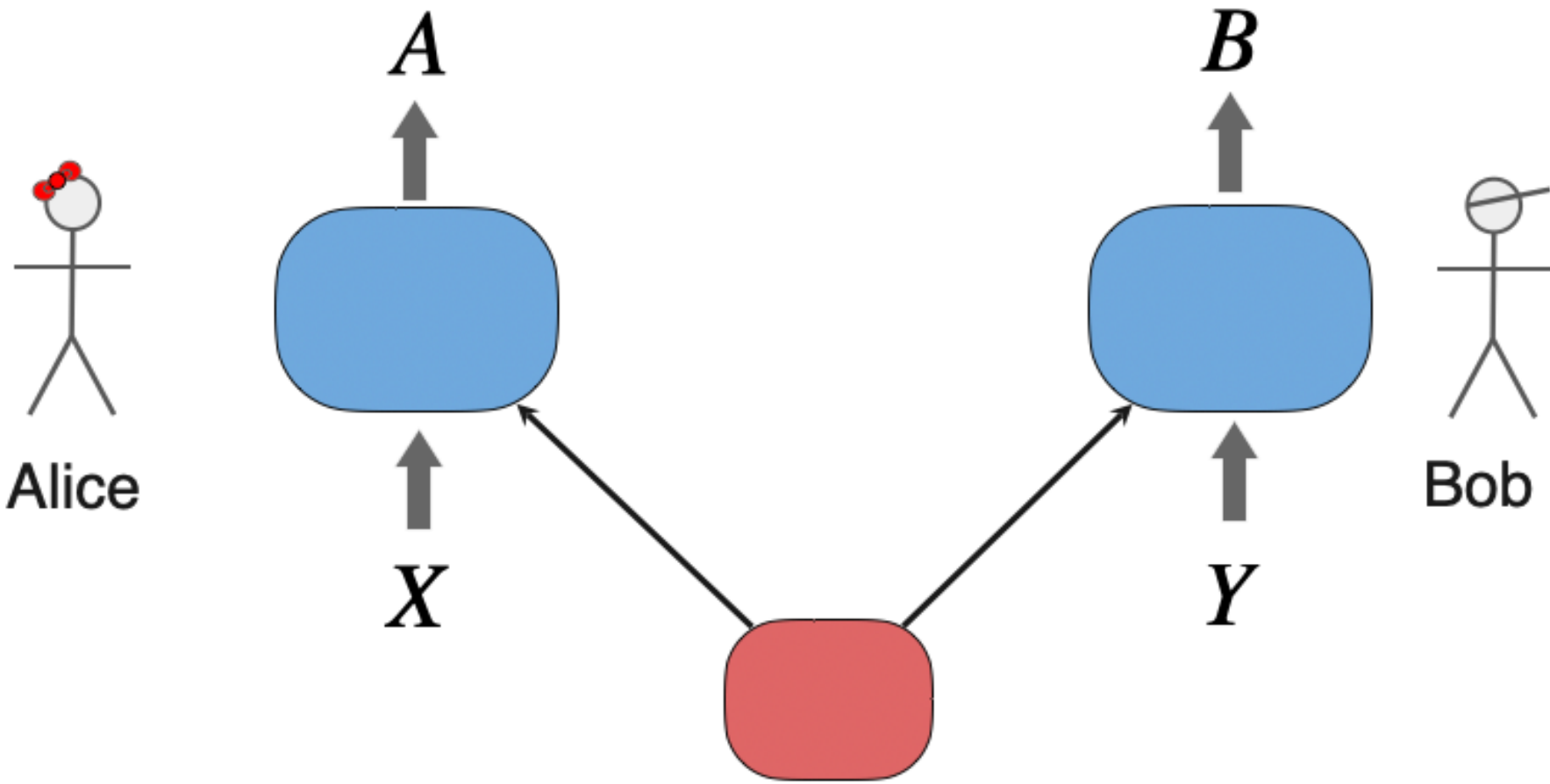
Markov condition

$$p(abxy) = \sum_{\lambda} p(a | x\lambda)p(b | y\lambda)p(x)p(y)p(\lambda)$$

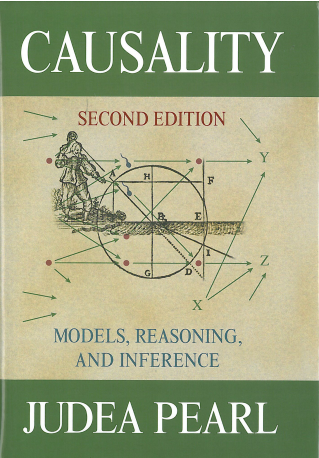
$\Downarrow$
 $A \perp Y | X$

$\Downarrow$
 $B \perp X | Y$

$\Downarrow$
Bell Inequalities

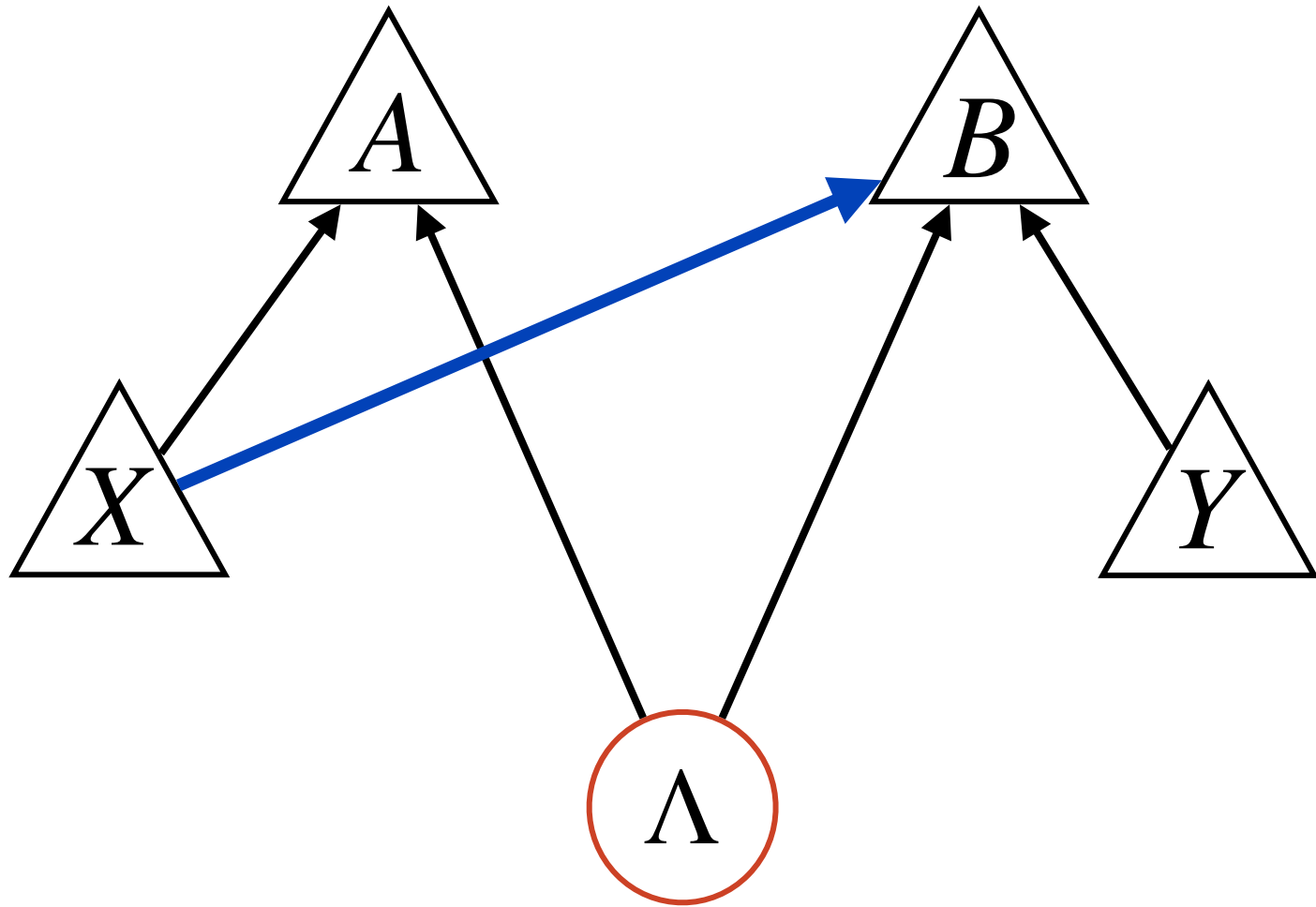


$A \perp Y | X$
 $B \perp X | Y$



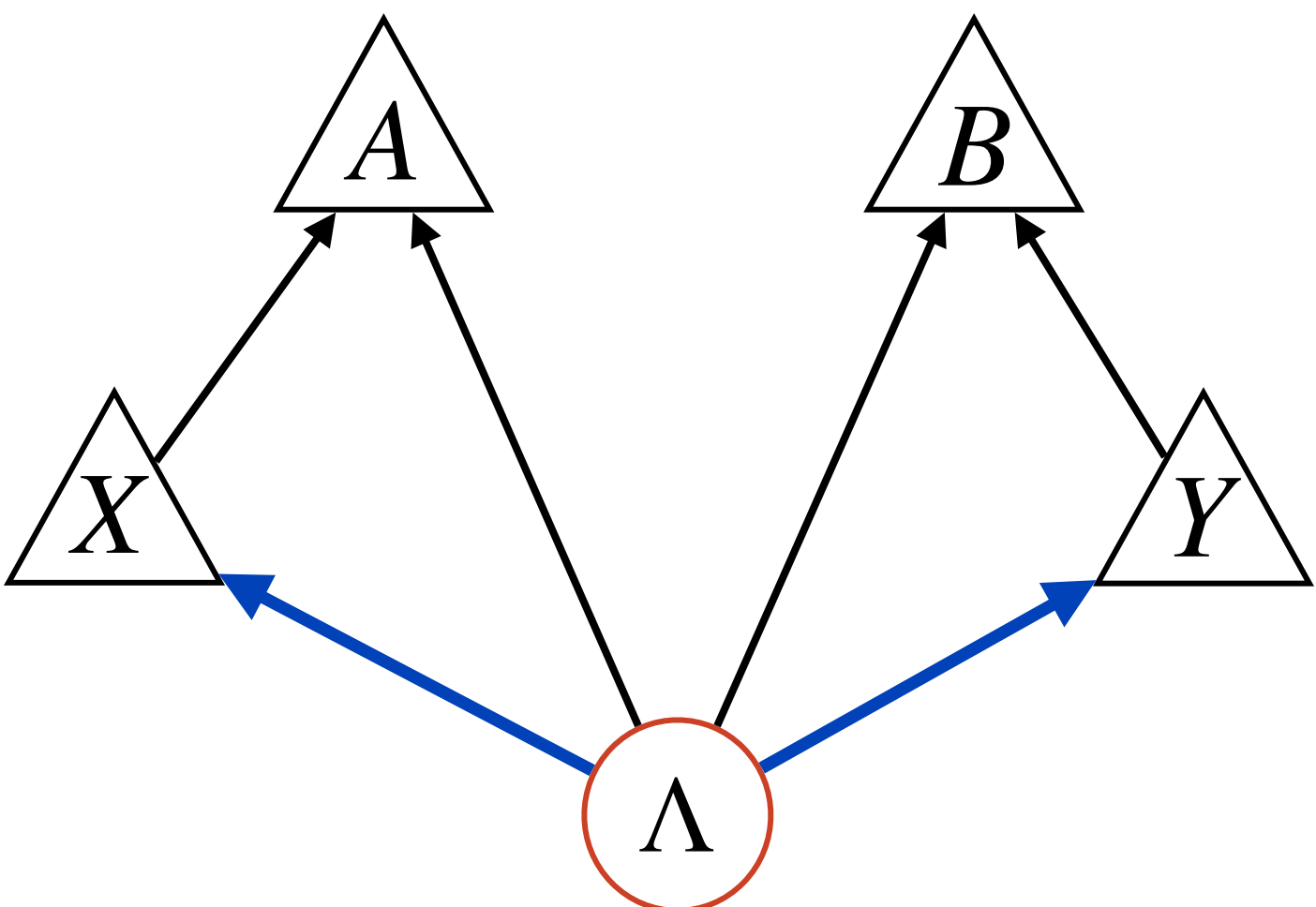
alternative causal models

superluminal causation



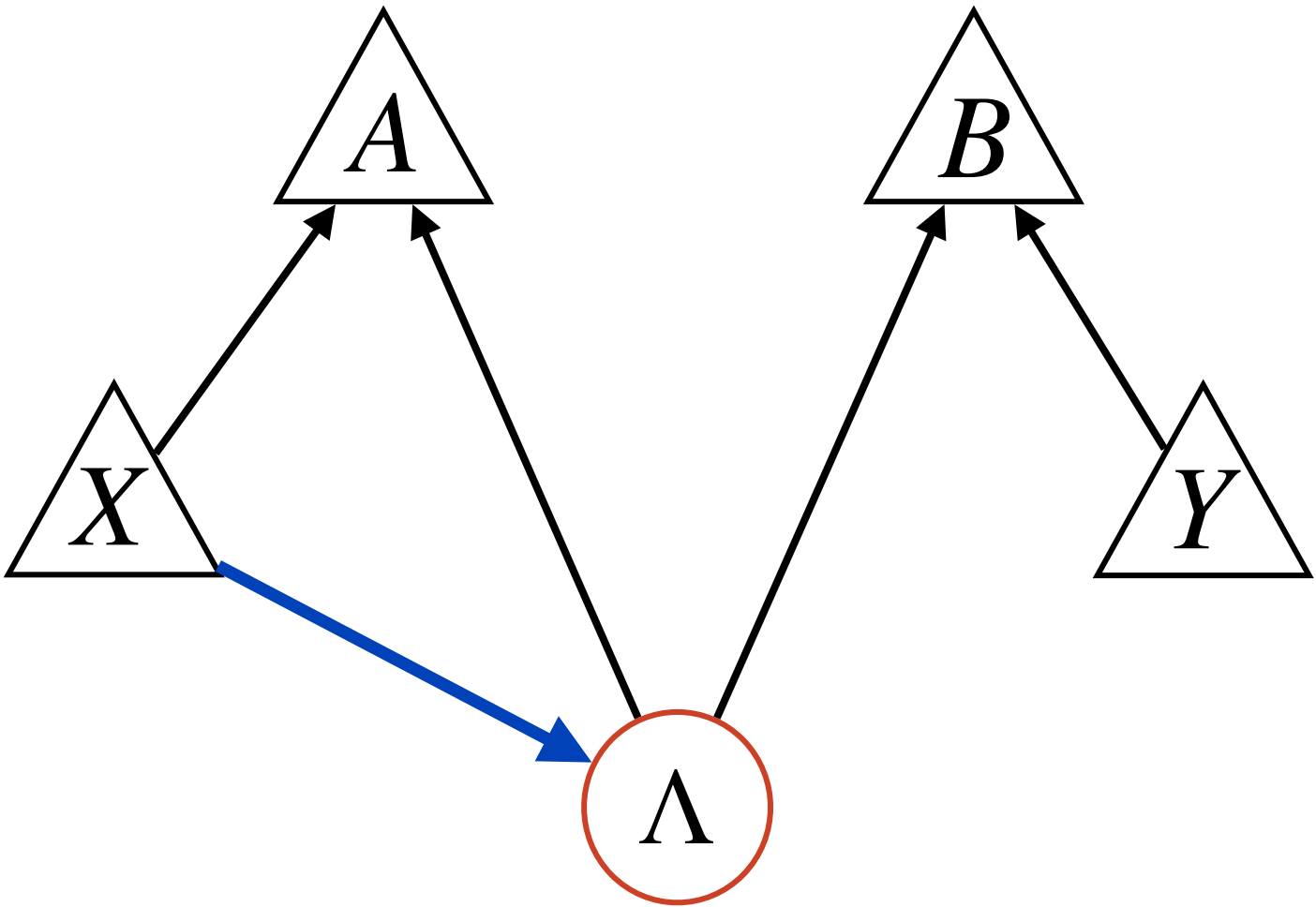
compatible with Bell inequality violations...

superdeterminism



BUT

retrocausality



in tension with Bell's assumptions (of course)

AND ALSO

finetuned explanations

no finetuning principle

$$A \perp B \mid C \iff A \perp_d B \mid C$$

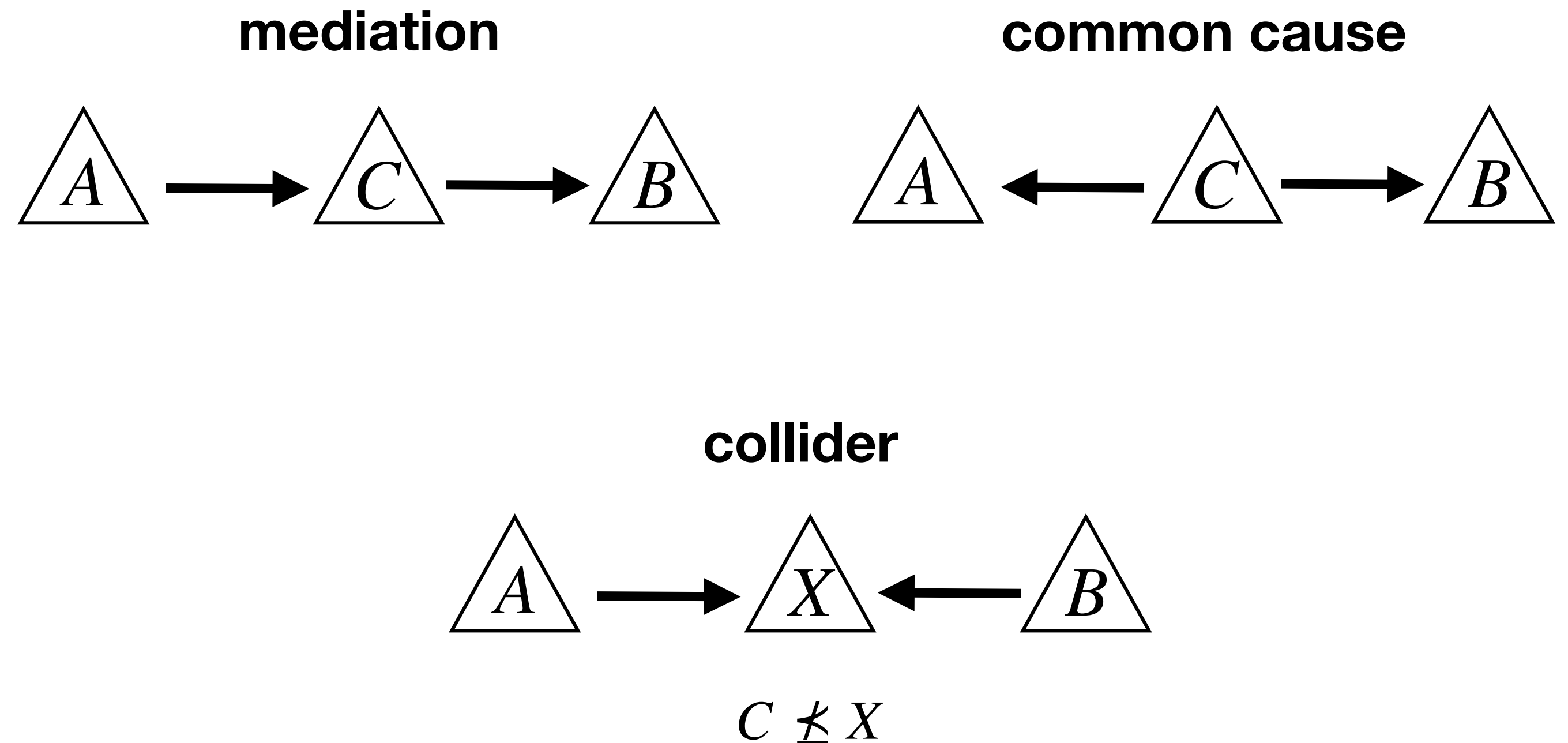
no finetuning principle

**every statistical independence in the data is
implied by the causal structure**

d -separation

$$A \perp_d B \mid C$$

C d -separates A and B
if it *blocks*
all paths from A and B



no finetuning principle

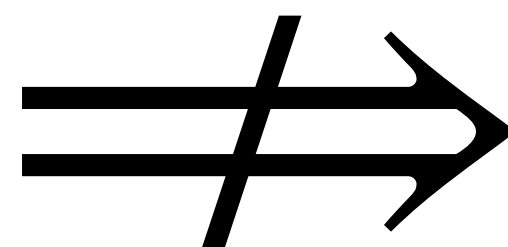
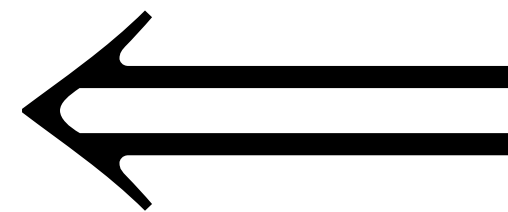
data

$$A \perp B \mid C$$

A and B are
statistically independent given C

$$p(ab \mid c) = p(a \mid c)p(b \mid c)$$

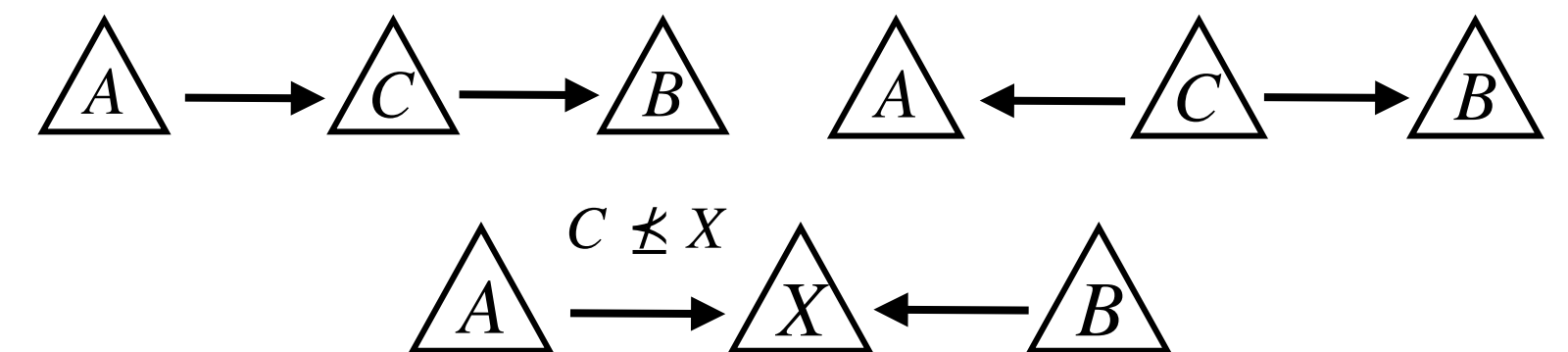
Markov condition



model

$$A \perp_d B \mid C$$

A and B are
 d -separated by C



no finetuning principle

data

$$A \perp B \mid C$$

*A and B are
statistically independent given C*

$$p(ab \mid c) = p(a \mid c)p(b \mid c)$$

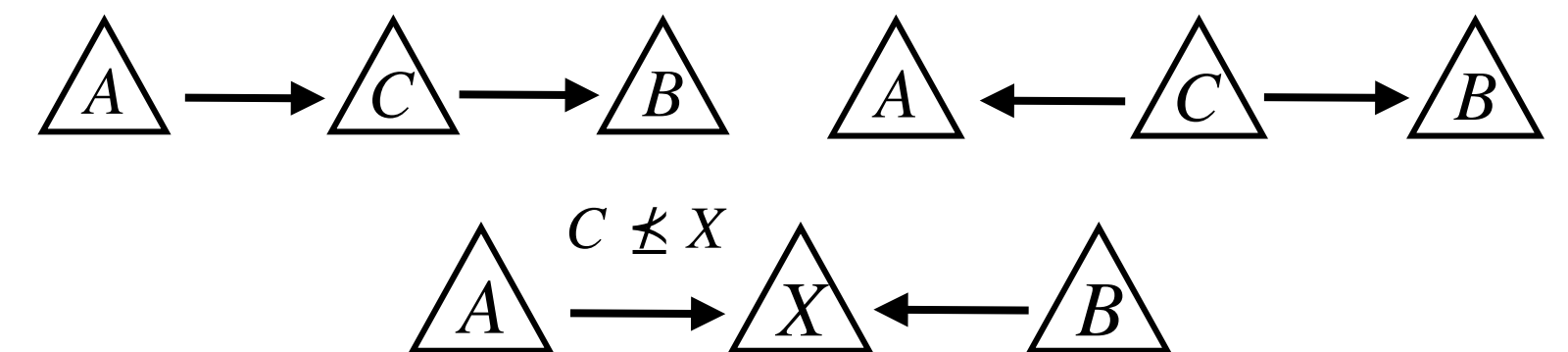
no finetuning



model

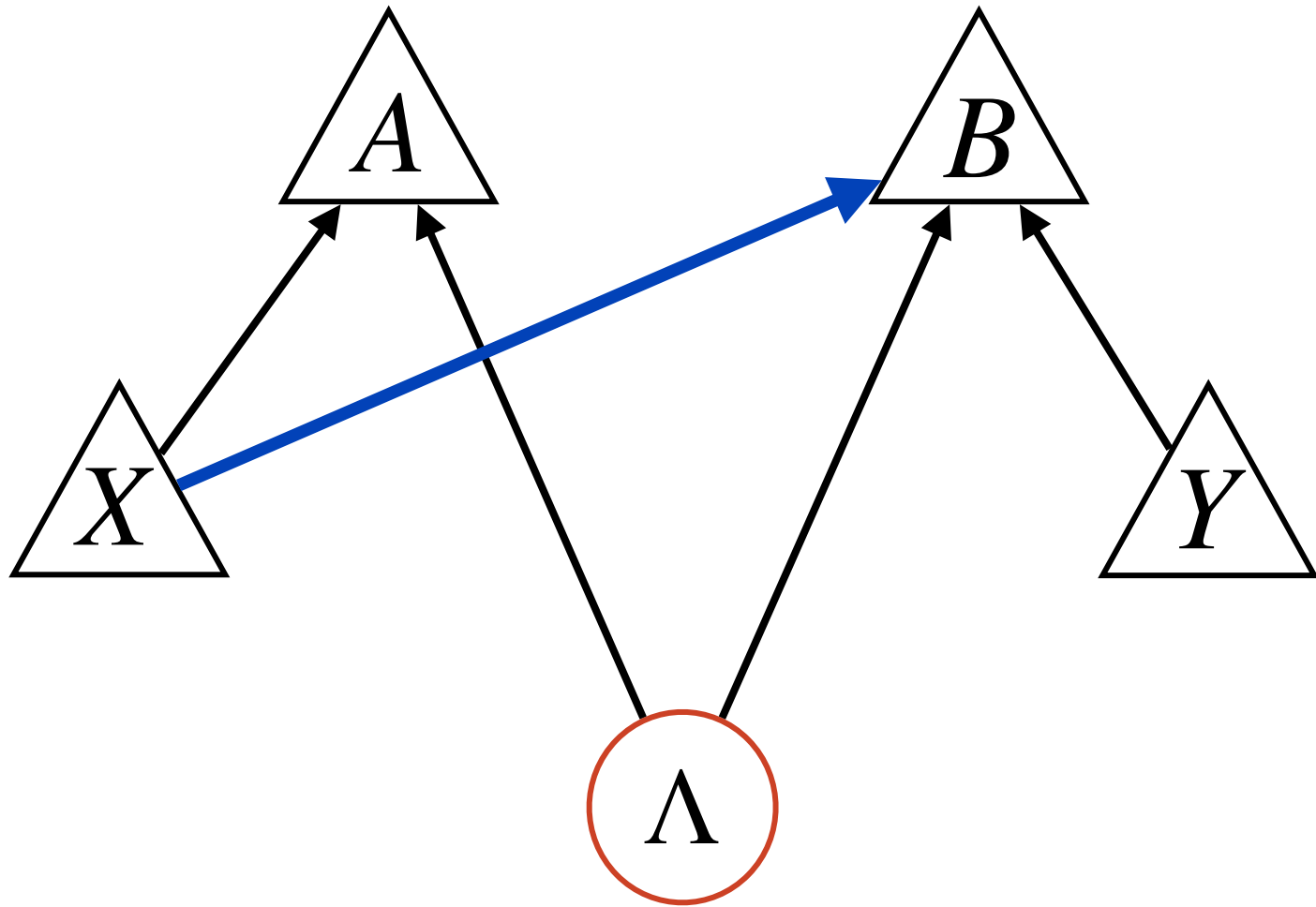
$$A \perp_d B \mid C$$

*A and B are
d-separated by C*

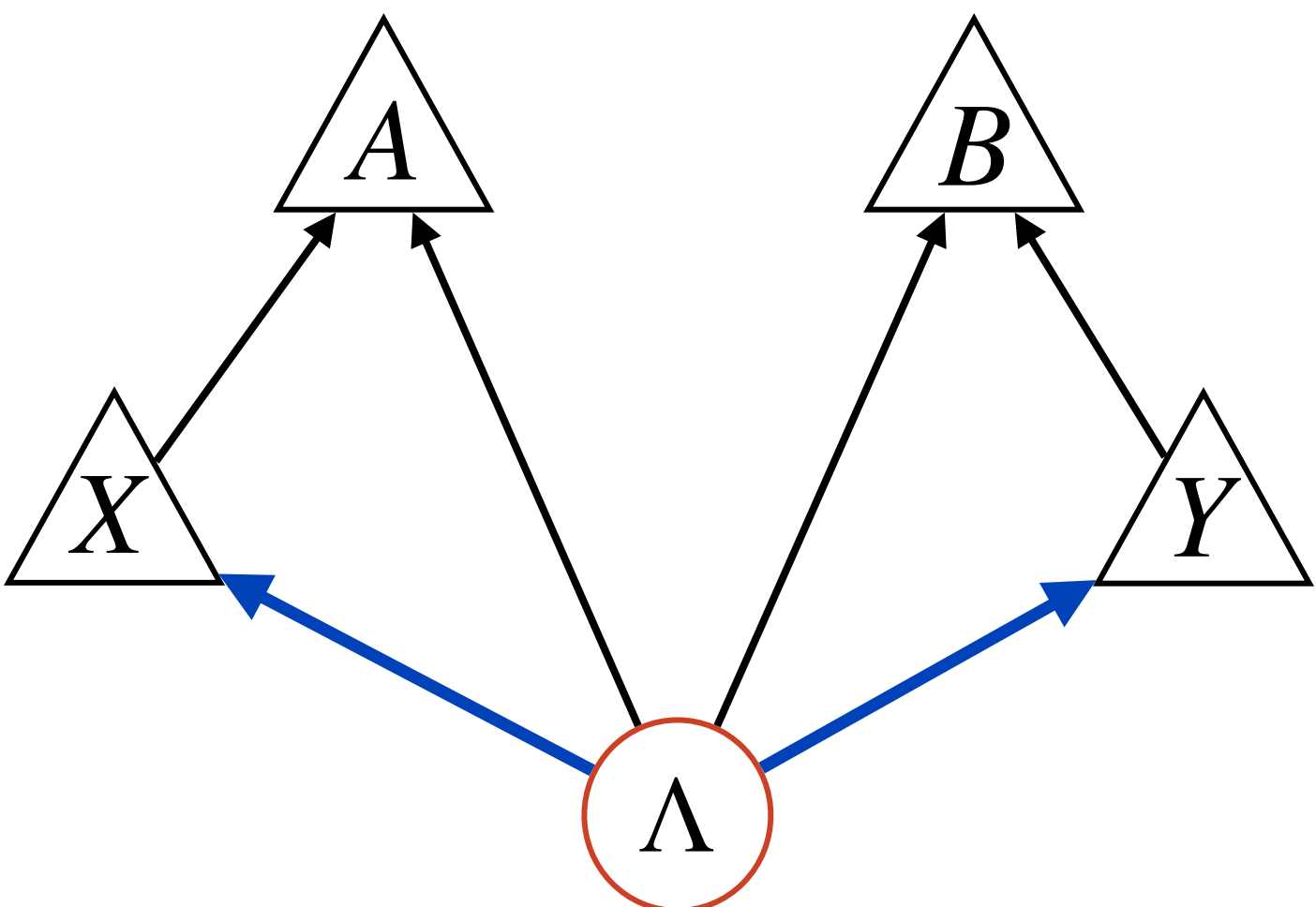


alternative causal models

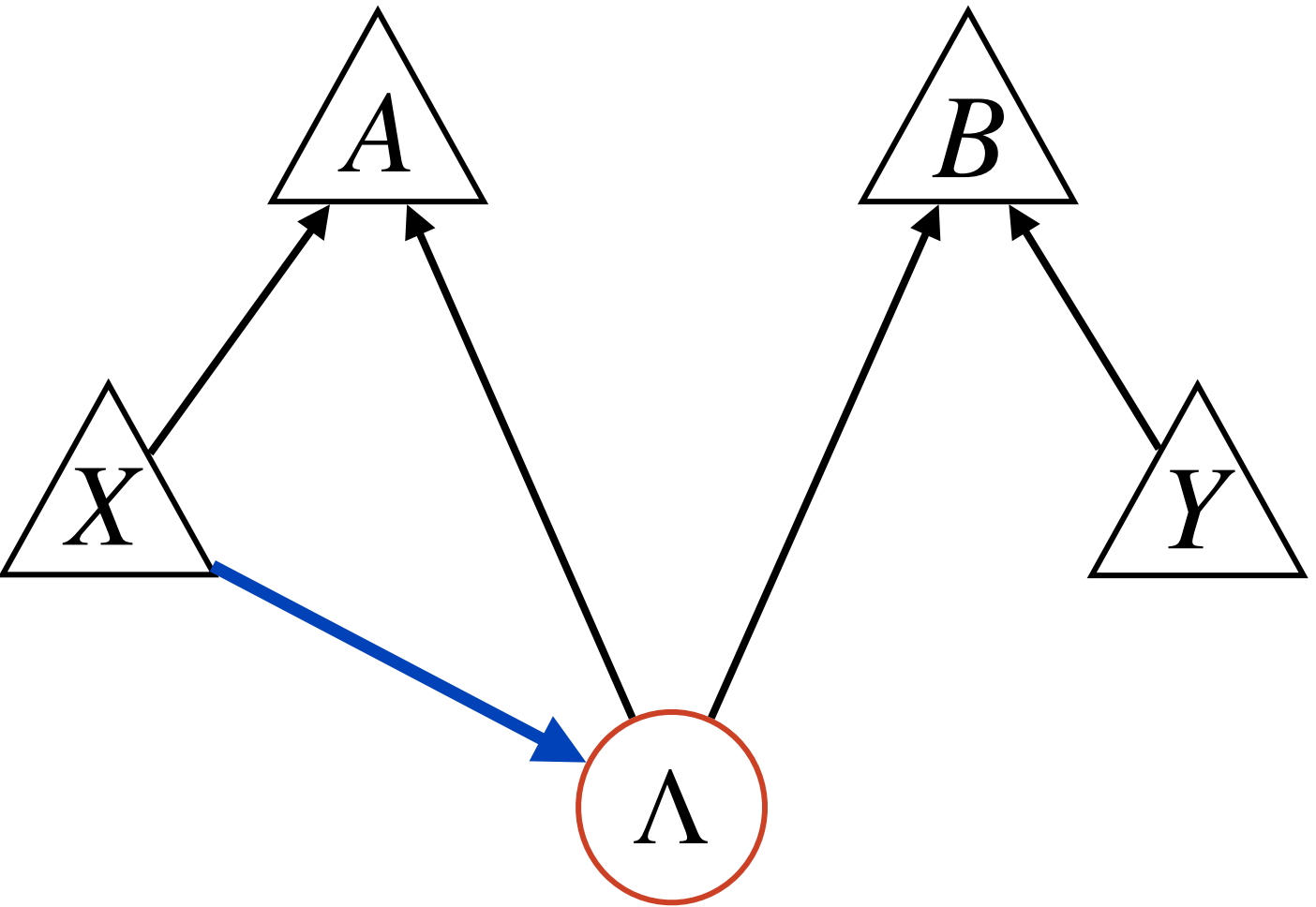
superluminal causation



superdeterminism



retrocausality



compatible with Bell inequality violations...

BUT

finetuned explanations

$$B \not\perp_d X \mid Y$$

requires more explanation

Wood-Spekkens theorem

PAPER • OPEN ACCESS

The lesson of causal discovery algorithms for quantum correlations: causal explanations of Bell-inequality violations require fine-tuning

Christopher J Wood and Robert W Spekkens

[New Journal of Physics, Volume 17, March 2015](#)

Citation Christopher J Wood and Robert W Spekkens 2015 *New J. Phys.* 17 033002

DOI 10.1088/1367-2630/17/3/033002

all classical causal models
for Bell inequality violations are finetuned

(no need for spacelike separation!)

$$\begin{aligned} A &\perp Y | X \\ B &\perp X | Y \end{aligned}$$

observations

no finetuning



$$\begin{aligned} A &\perp_d Y | X \\ B &\perp_d X | Y \end{aligned}$$

causal structure

Markov



Bell inequalities

observations

Wood-Spekkens solution

PAPER • **OPEN ACCESS**

The lesson of causal discovery algorithms for quantum correlations: causal explanations of Bell-inequality violations require fine-tuning

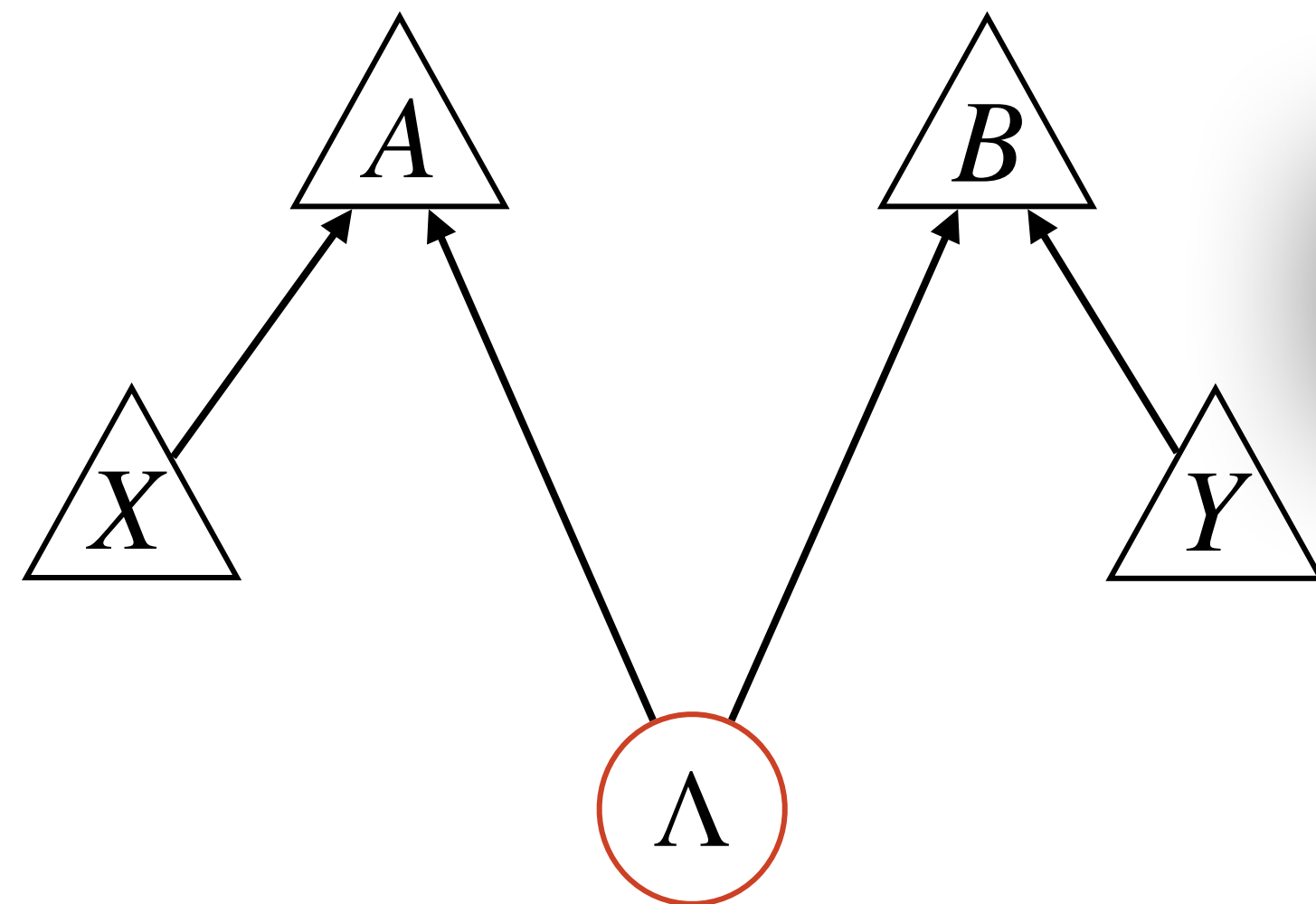
Christopher J Wood and Robert W Spekkens

[New Journal of Physics](#), Volume 17, March 2015

Citation Christopher J Wood and Robert W Spekkens 2015 *New J. Phys.* 17 033002

DOI 10.1088/1367-2630/17/3/033002

classical causal modelling

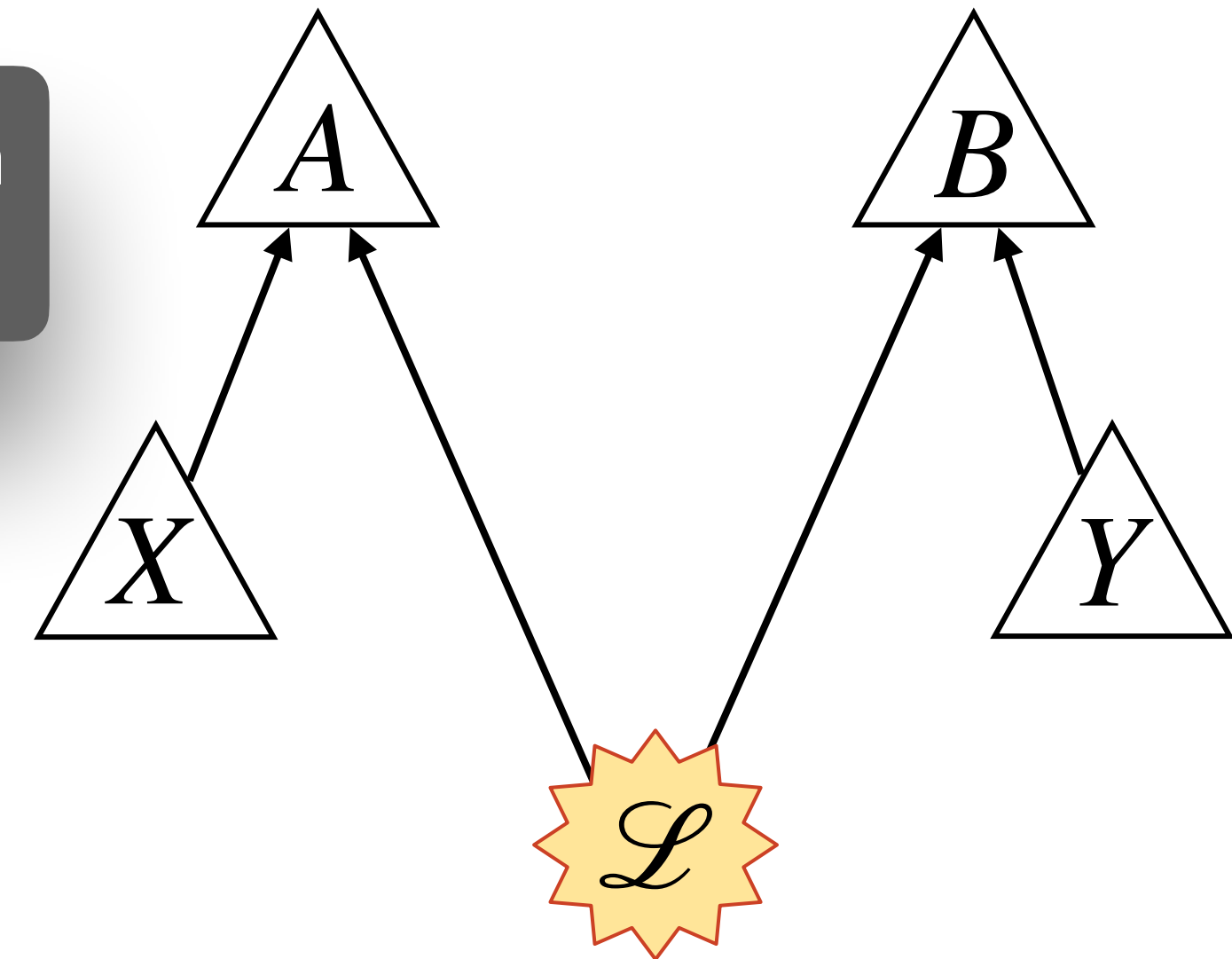


relativistic
causal arrow

Reichenbach
principle

local causality

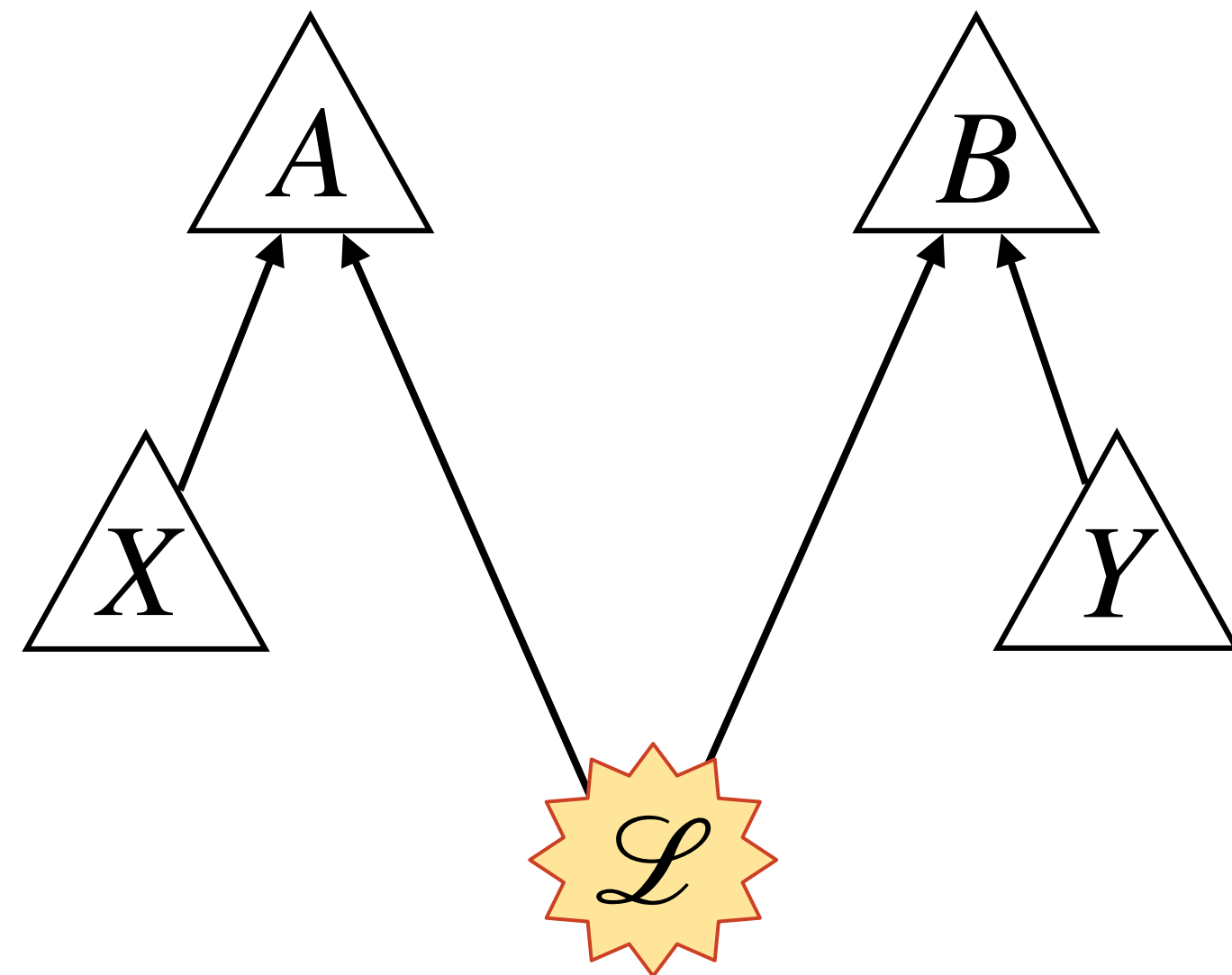
quantum causal modelling



$$p(abxy) = \sum_{\lambda} p(a | x\lambda)p(b | y\lambda)p(x)p(y)p(\lambda)$$

$$p(abxy) = \text{tr} \left[E_x^a E_y^b \rho_{\mathcal{L}} \right] p(x)p(y)$$

Wood-Spekkens solution



$$\Rightarrow A \perp Y | X$$

$$\Rightarrow B \perp X | Y$$

$\nRightarrow$ **Bell inequalities**

$\Rightarrow$ **Tsirelson bound**

$$p(abxy) = \text{tr} \left[E_x^a E_y^b \rho_{\mathcal{L}} \right] p(x)p(y)$$

relativistic
causal arrow

Reichenbach
principle

local causality

Wigner and post-quantum causal models

 quantum

2024-09-26, volume 8, page 1485

Relating Wigner's Friend Scenarios to
Nonclassical Causal Compatibility, Monogamy
Relations, and Fine Tuning



**Yìlè
Yīng**



**Marina
Maciel Ansanelli**



**Elie
Wolfe**



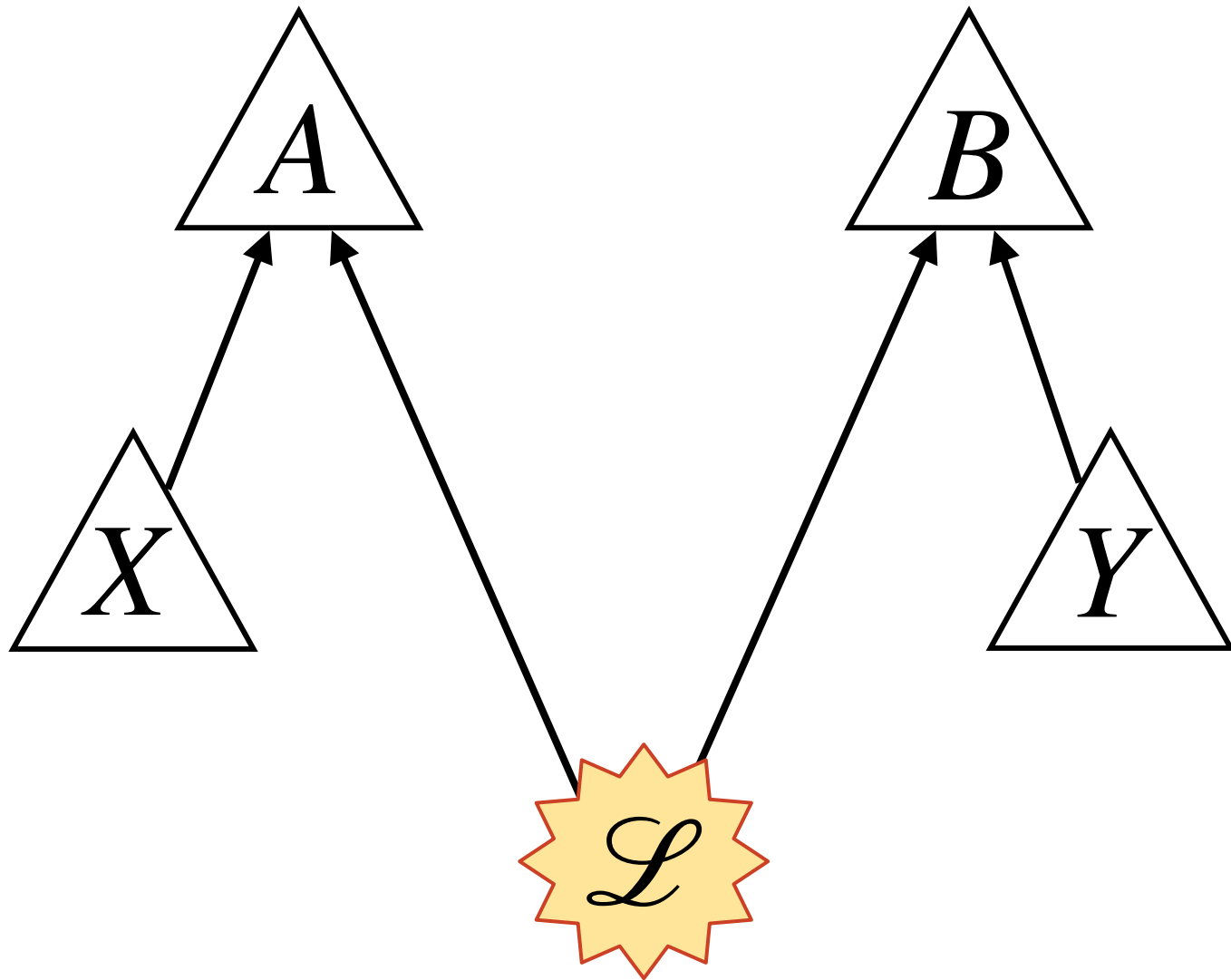
**David
Schmid**



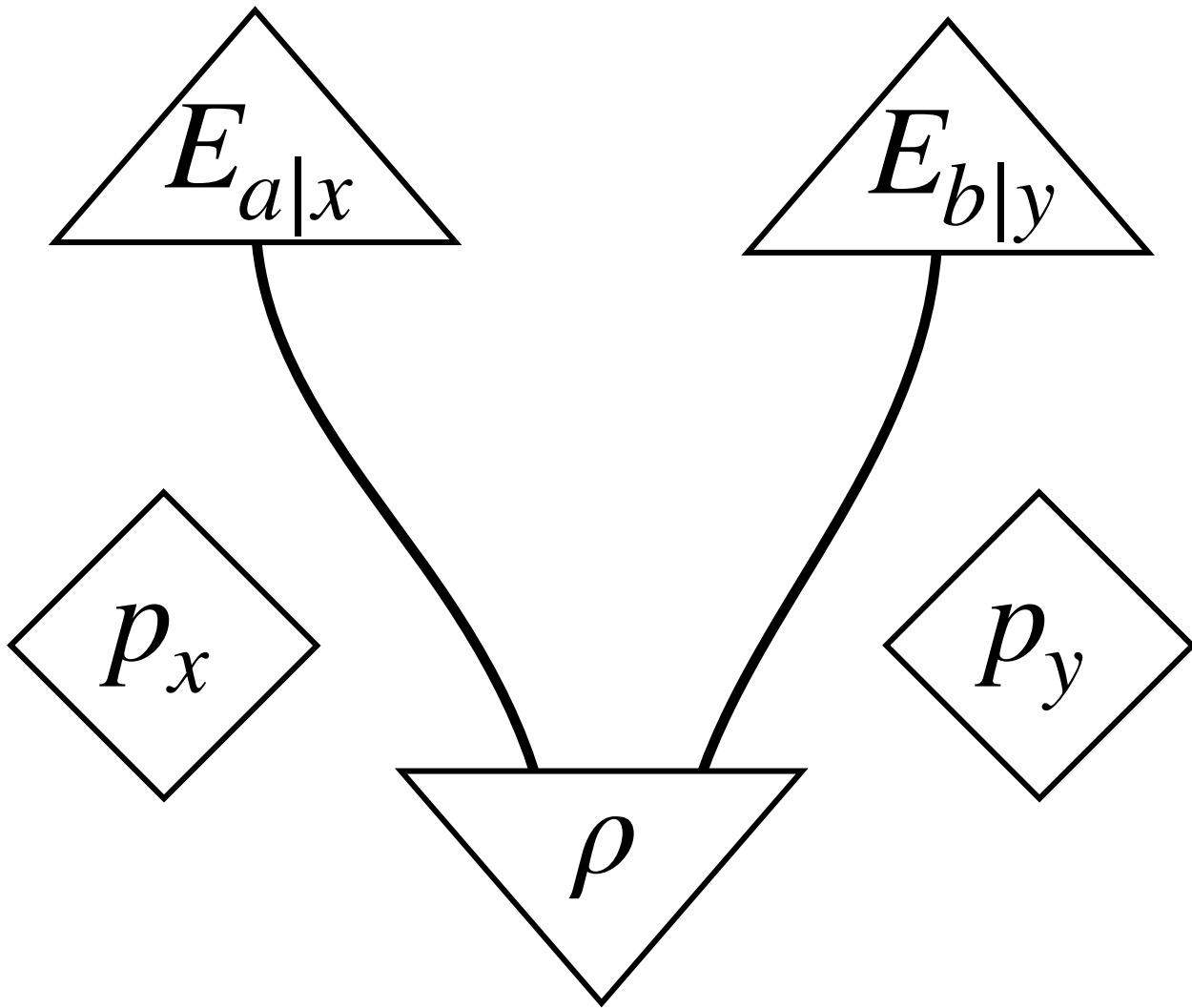
**Eric Gama
Cavalcanti**

post-quantum causal modelling

DAG



GPT circuit



generalised
Markov condition



A probability distribution over observed nodes, denoted as $P(\text{obs}(\mathcal{G}))$, is GPT-compatible¹⁹ with a given causal structure $\mathcal{G}$ if and only if it can be generated by a GPT in the way prescribed by $\mathcal{G}$, namely, if and only if there exists a GPT $\mathcal{T}$ such that:

- a system in $\mathcal{T}$ is associated to each edge that starts from a latent node in $\mathcal{G}$,
- for each latent node Y and for any value of its observed parents, denoted $\text{opa}(Y)$, there is a channel $\mathcal{C}_Y(\text{opa}(Y))$ in $\mathcal{T}$ from the systems associated with latent-originating edges incoming to Y to the composite system associated with all edges outgoing from Y ,
- for every value x of an observed node X , and for any value $\text{opa}(X)$ of its observed parents $\text{opa}(X)$, there is an effect $\mathcal{E}_X(x|\text{opa}(X))$ in $\mathcal{T}$ on the system composed of all systems associated with edges incoming in X , such that $\sum_x \mathcal{E}_X(x|\text{opa}(X))$ is the unique deterministic effect on the systems associated to edges coming from latent nodes to X ,
- $P(\text{obs}(\mathcal{G}))$ is the probability obtained by wiring the various tests $\mathcal{E}_X(x|\text{opa}(X))$ and channels $\mathcal{C}_Y(\text{opa}(Y))$.

Note that the theory $\mathcal{T}$ may contain several system types, e.g., including also classical ones. According to these definitions above, an observed node with no latent parents is simply associated with a (conditional) probability distribution (a set of effects on the trivial system that sum to the unique deterministic effect on the trivial system), while a latent node with no latent parents is associated to a classically-controlled state over the relevant systems (i.e., a controlled deterministic channel from the trivial system).

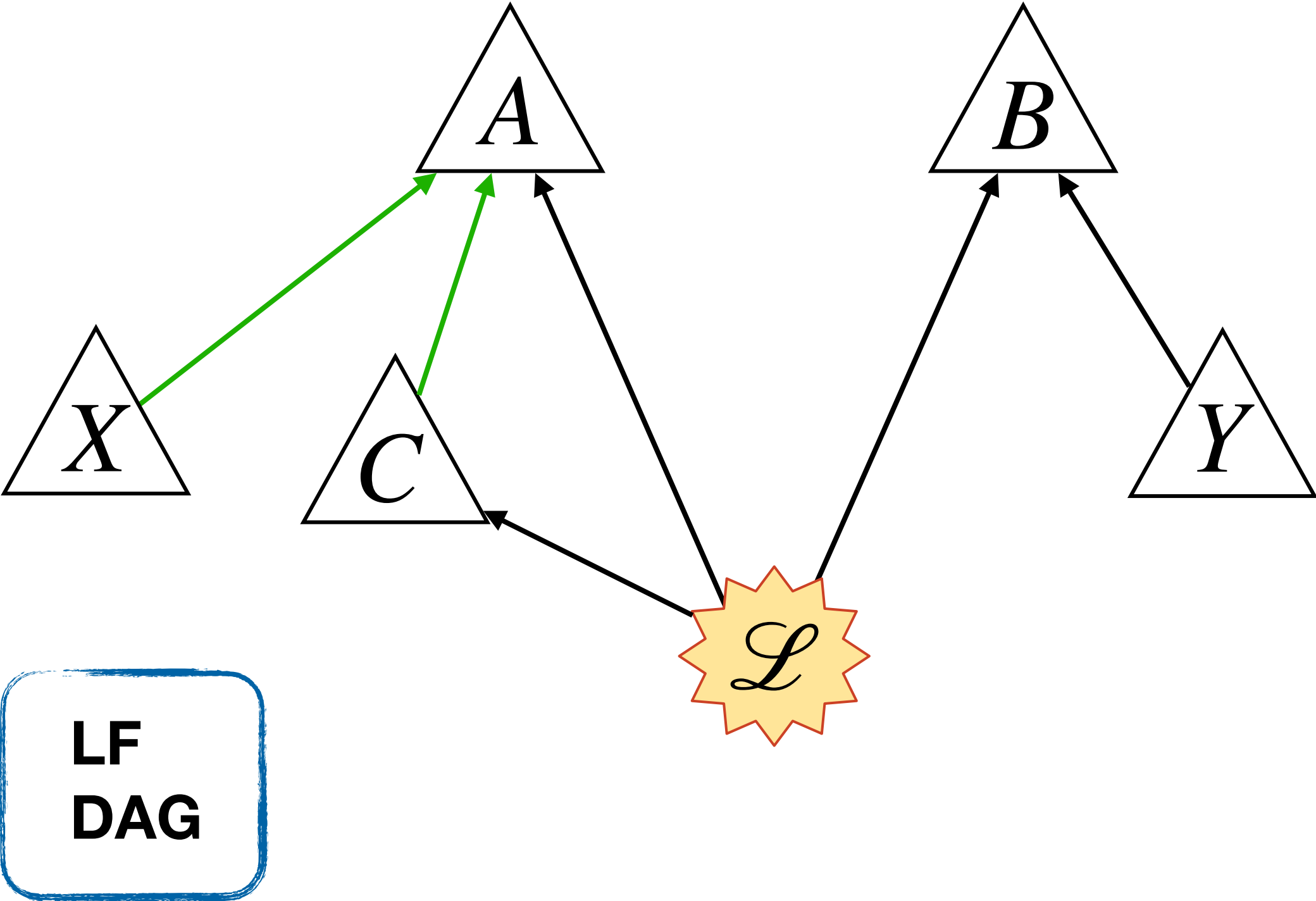
$$p(abxy) = (E_{a|x} \otimes E_{b|y})[\rho] p(x)p(y)$$

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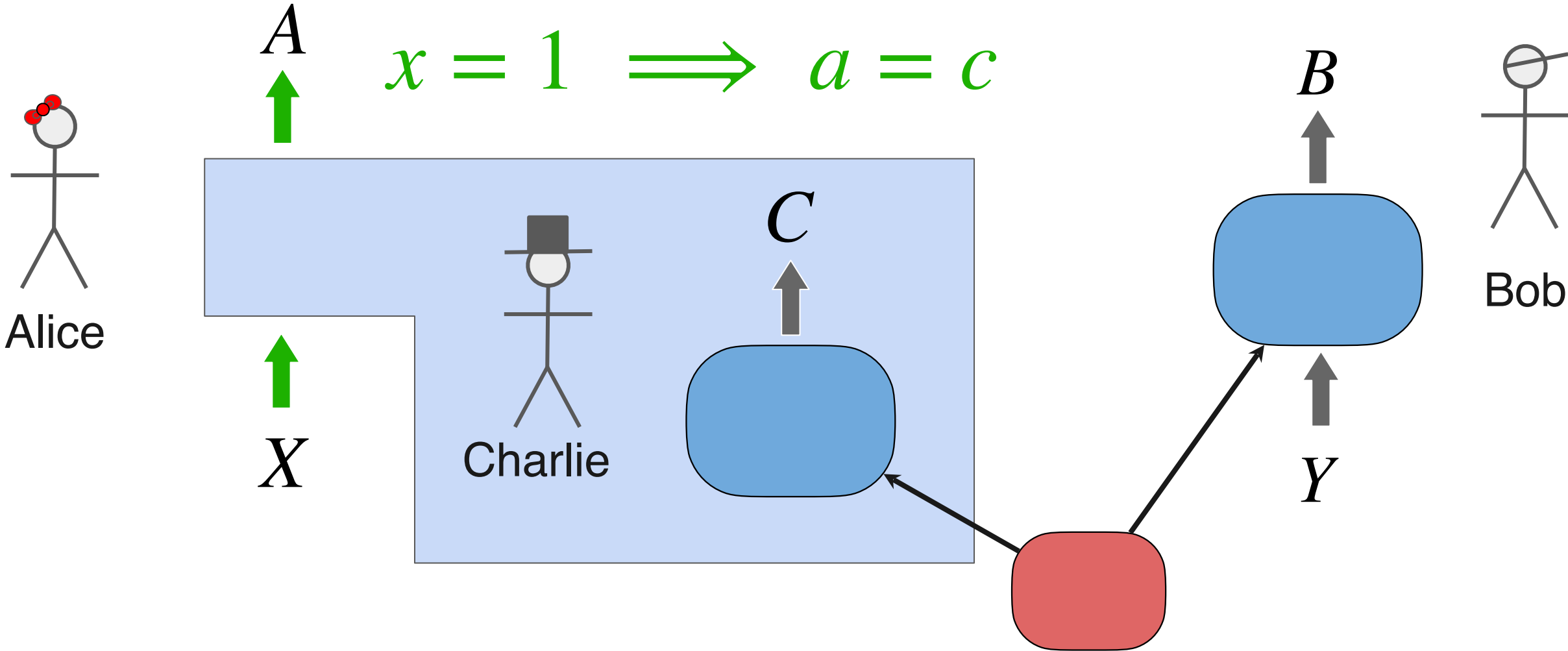
Theory-independent limits on correlations from generalized Bayesian networks

To cite this article: Joe Henson *et al* 2014 *New J. Phys.* **16** 113043

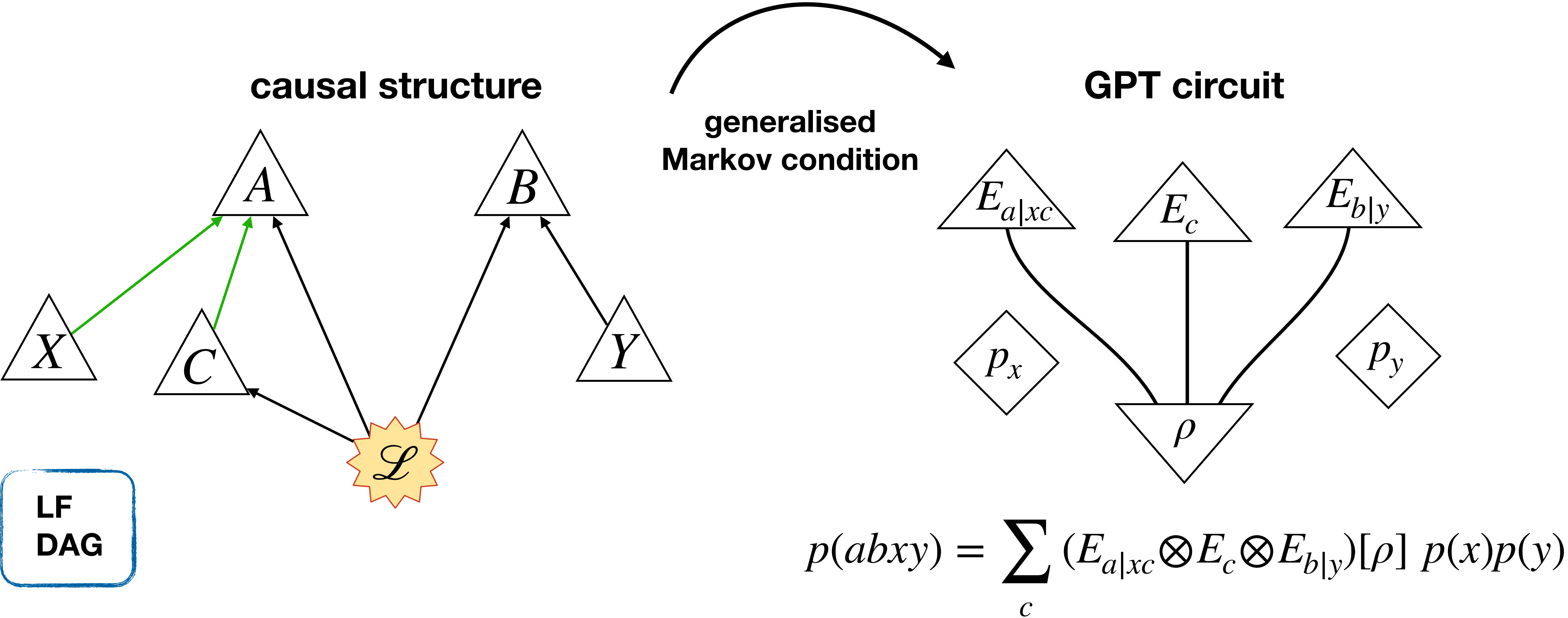
LF DAG



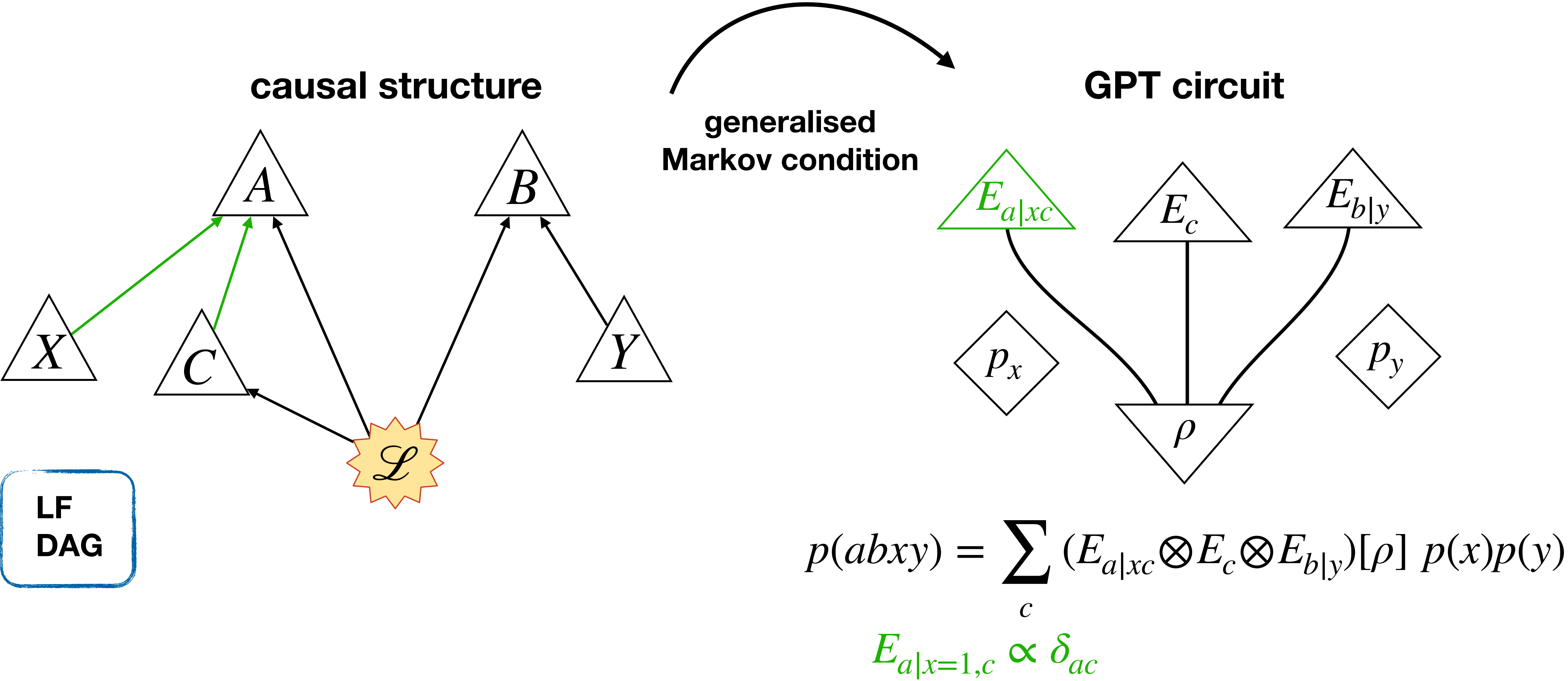
$$A \perp Y|X$$
$$B \perp X|Y$$
$$C \perp Y|x = 1$$



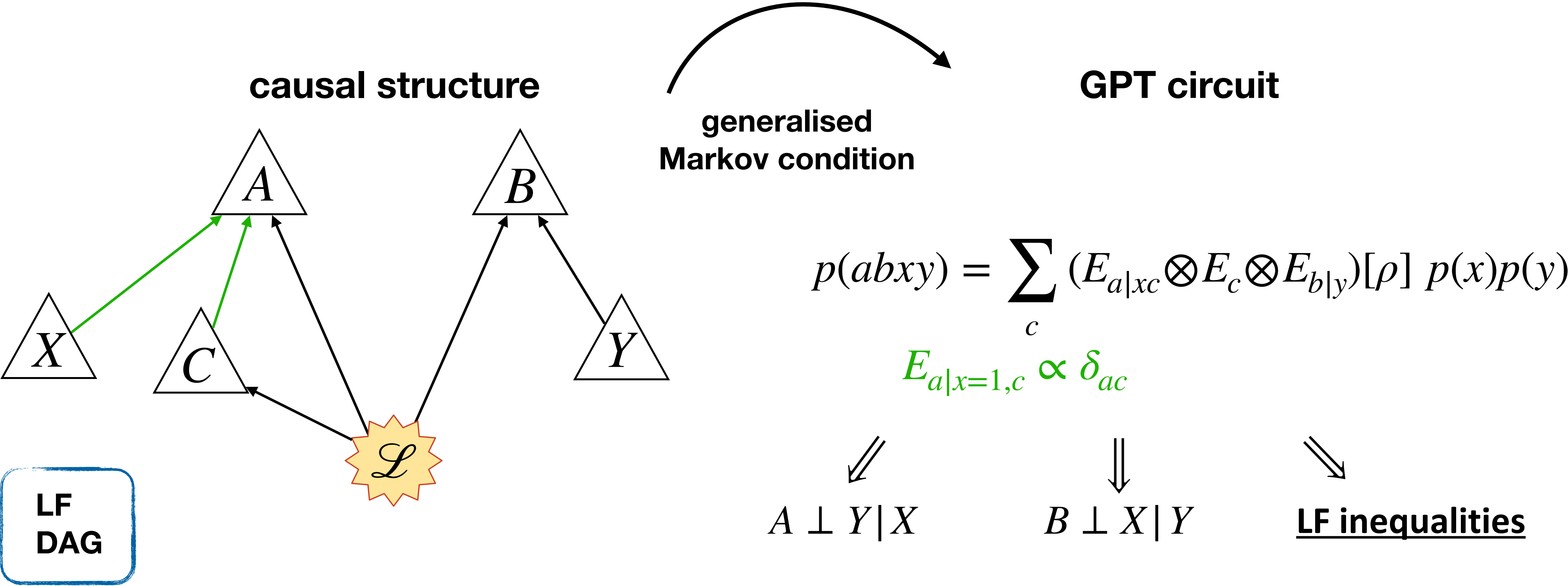
LF DAG



LF DAG

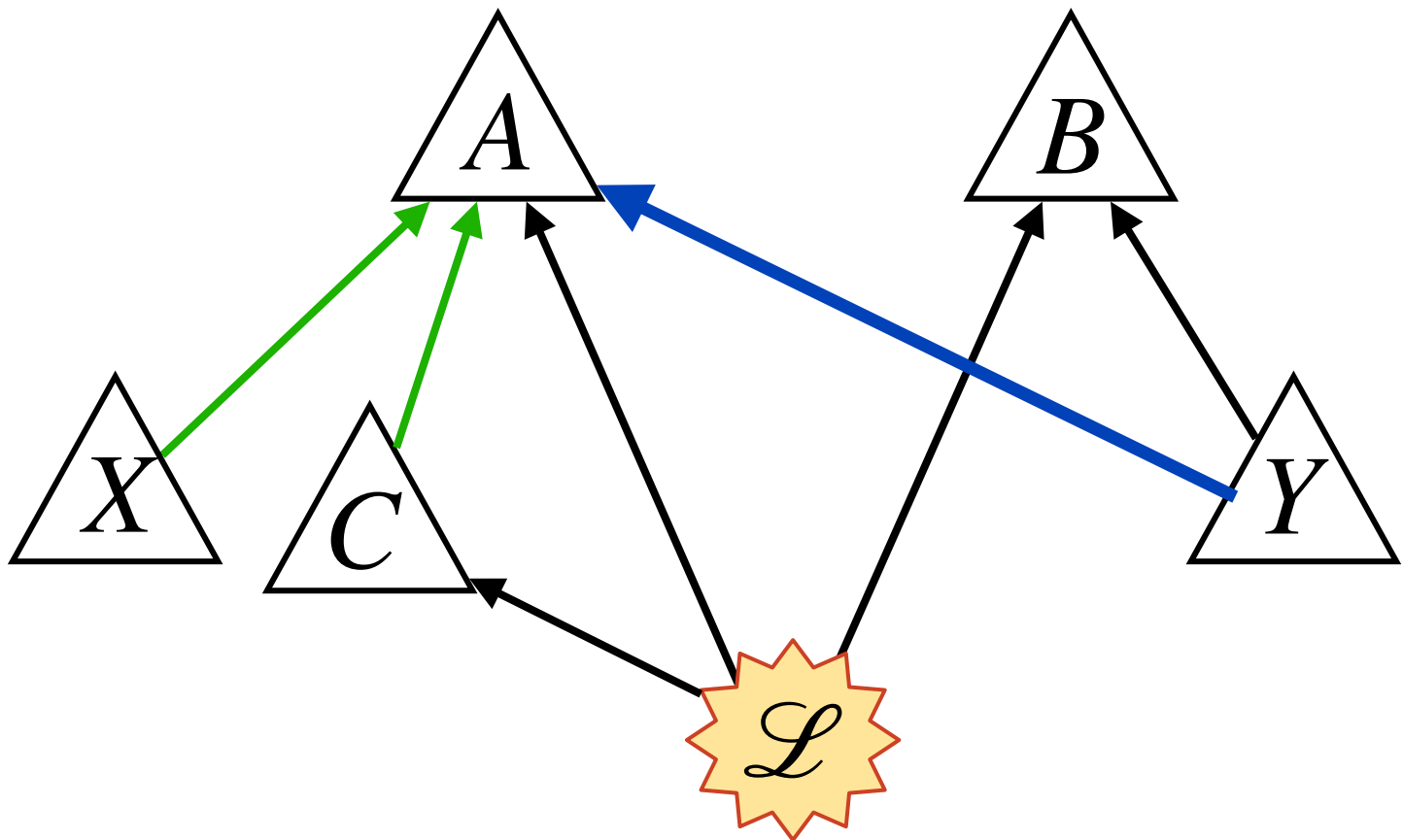


LF DAG no good



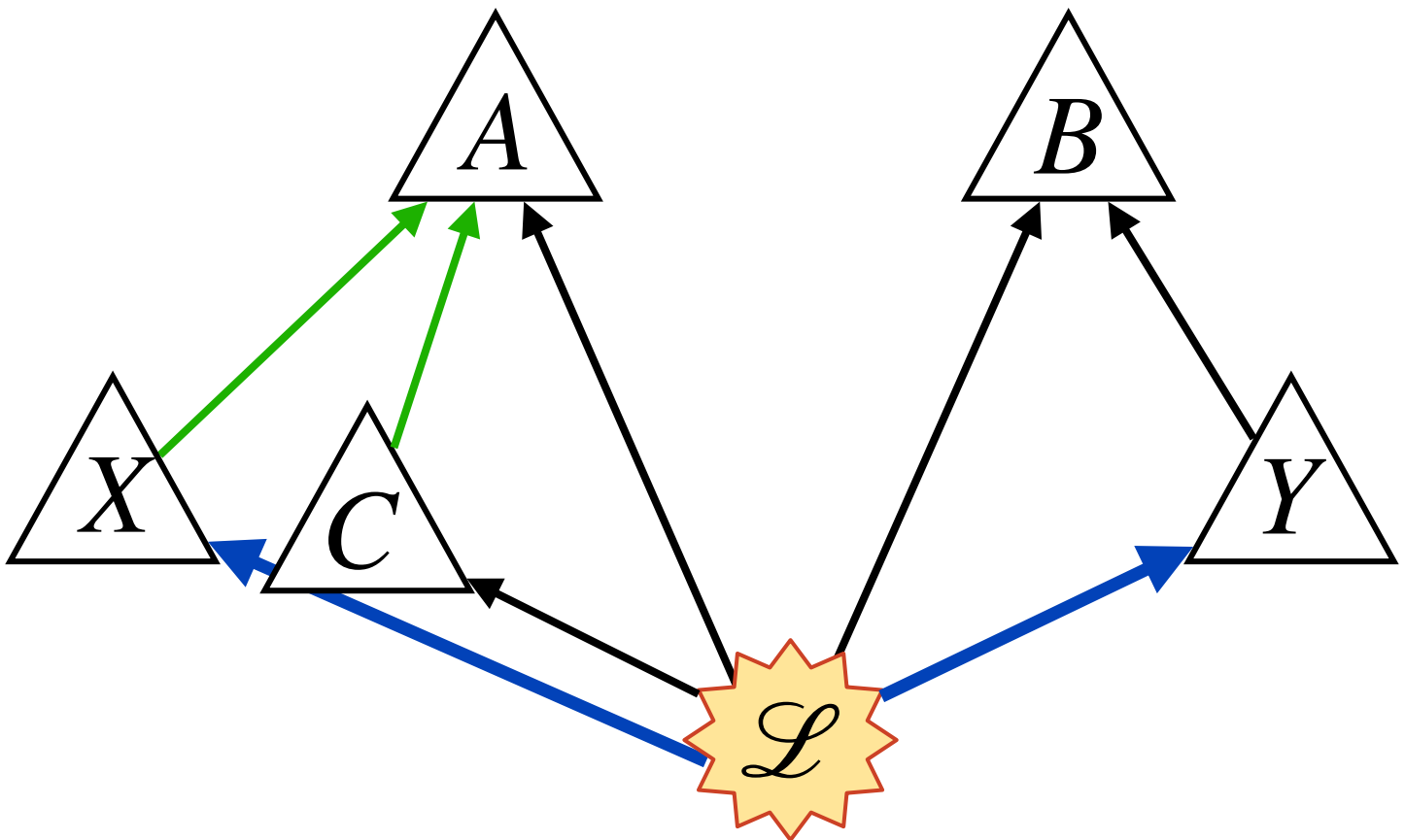
alternative causal models

superluminal causation



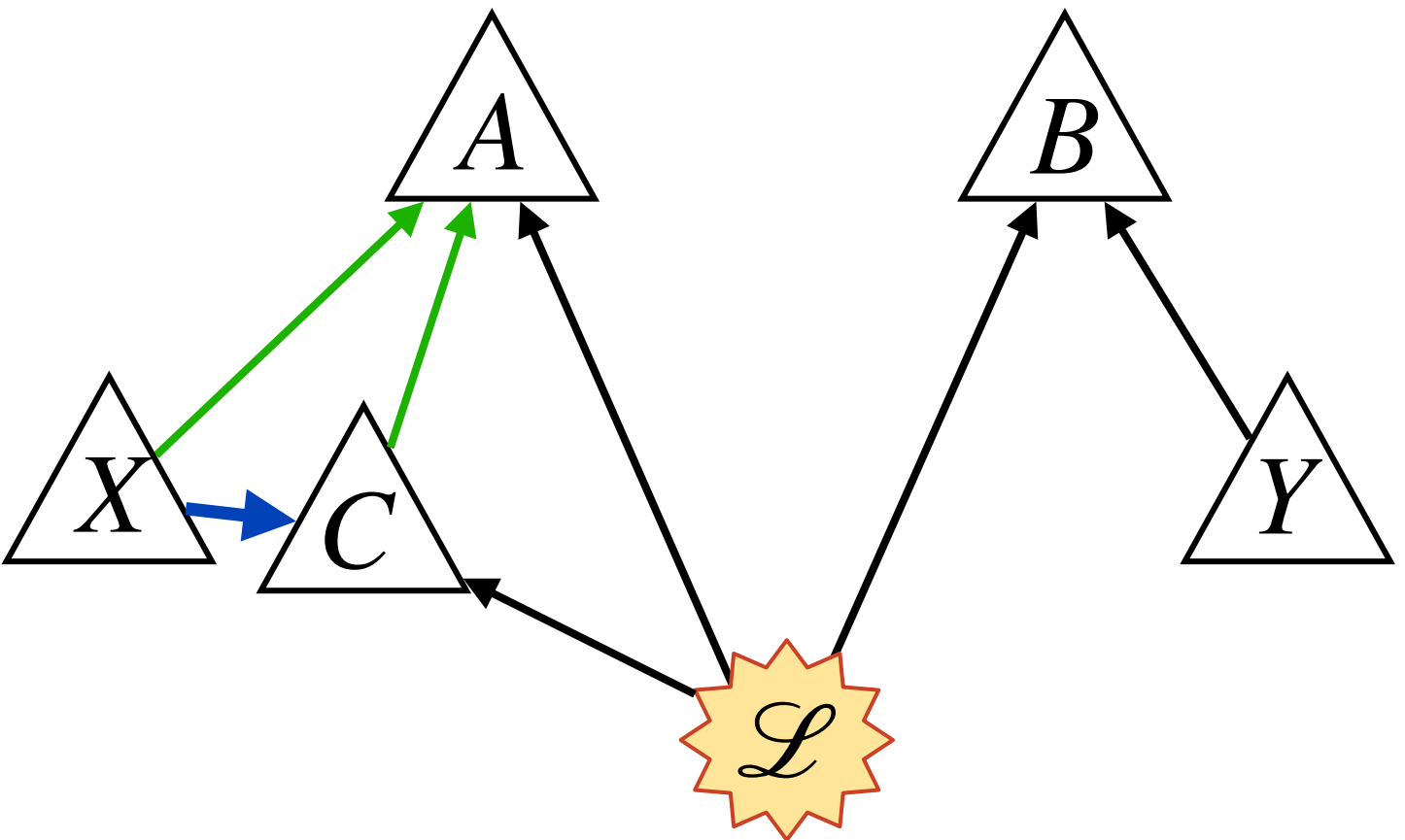
allow for LF inequality violations

superdeterminism



BUT

retrocausality



in tension with LF assumptions (of course)

AND ALSO

finetuned explanations

our theorem

all GPT-causal models
for LF inequality violations are finetuned

(no need for spacelike separation!)

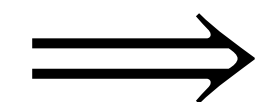
observations

$$A \perp Y | X$$

$$B \perp X | Y$$

$$C \perp XY$$

no finetuning



causal structure

$$A \perp_d Y | X$$

$$B \perp_d X | Y$$

$$C \perp_d XY$$

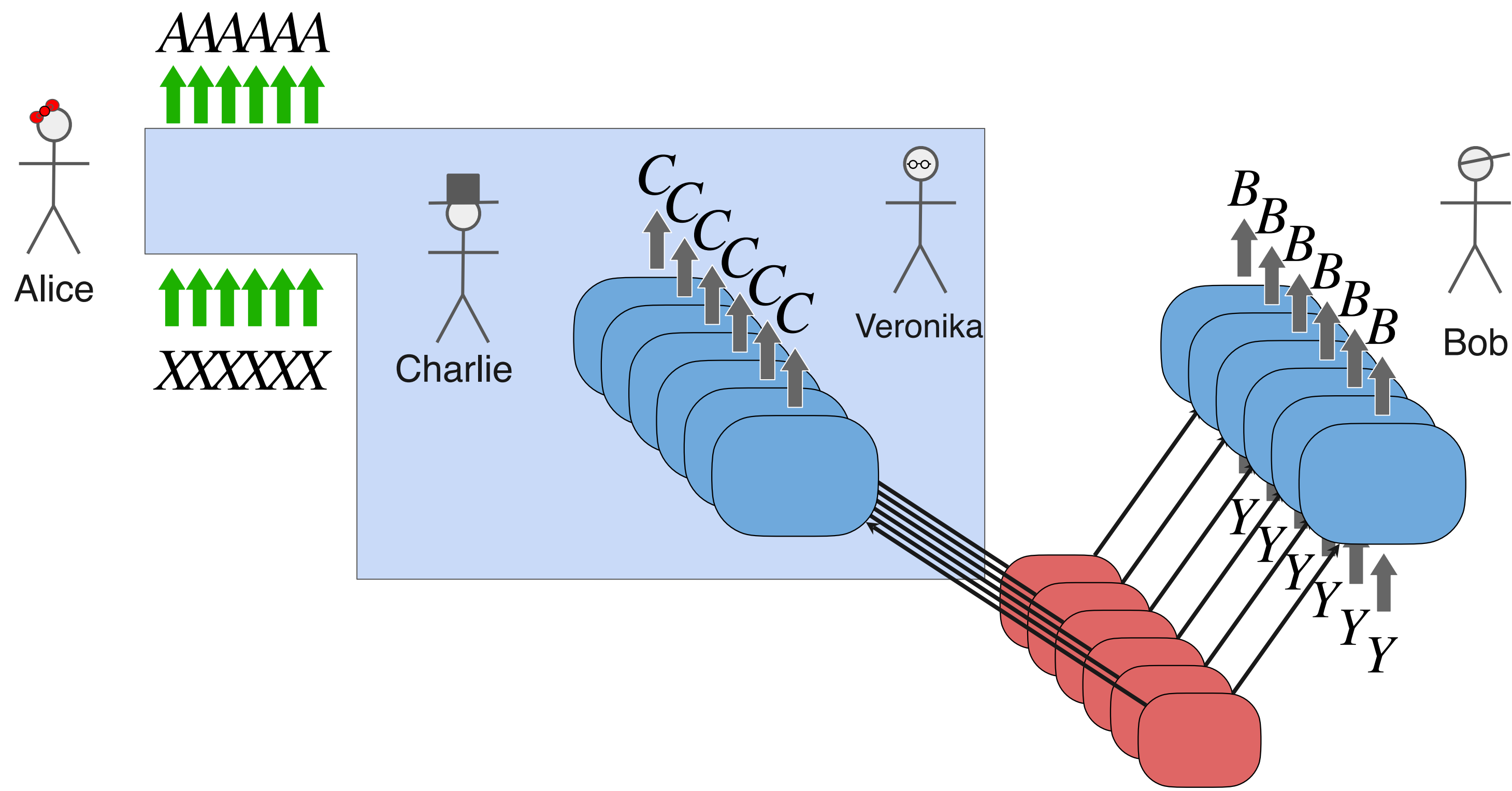
generalised
Markov



observations

LF inequalities

Veronika protocol

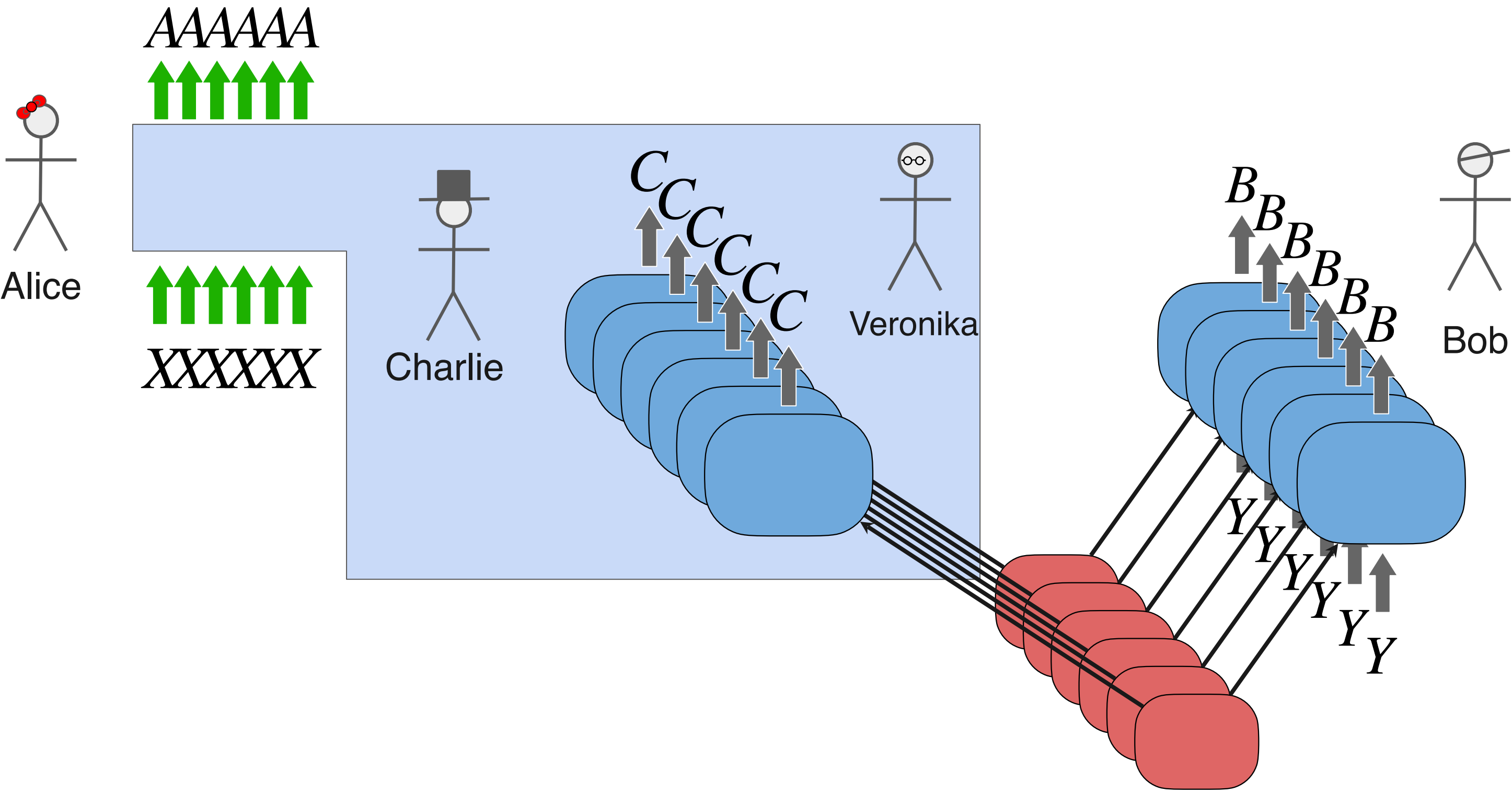


$C \perp XY \text{ ?}$



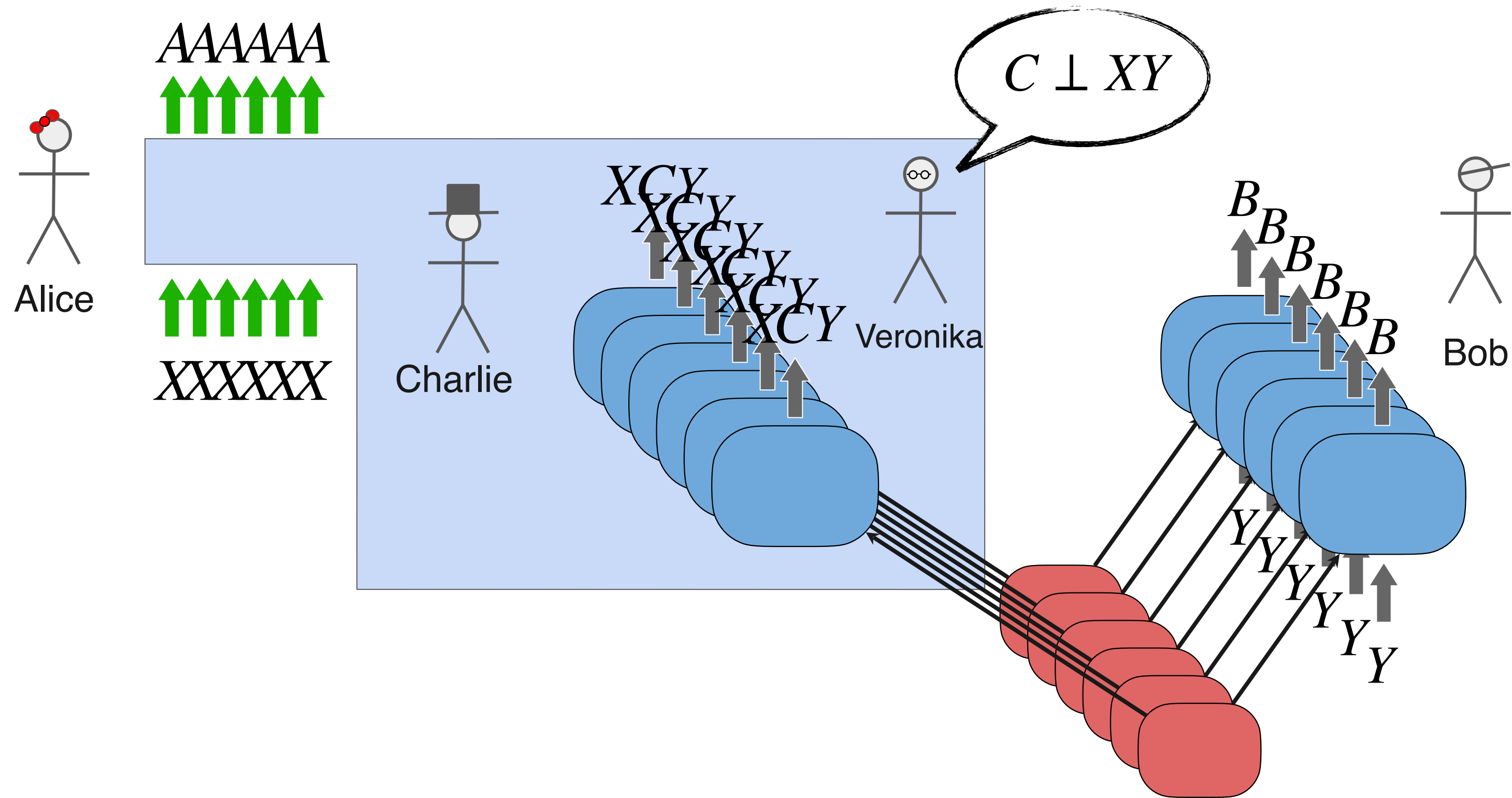
Veronika Bauman

Veronika protocol





Veronika protocol



$C \perp XY$?

our theorem

all GPT-causal models
for LF inequality violations are finetuned

(no need for spacelike separation!)

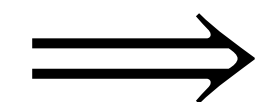
observations

$$A \perp Y | X$$

$$B \perp X | Y$$

$$C \perp XY$$

no finetuning



causal structure

$$A \perp_d Y | X$$

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generalised
Markov



observations

LF inequalities

our paper

 quantum

2024-09-26, volume 8, page 1485

Relating Wigner's Friend Scenarios to
Nonclassical Causal Compatibility, Monogamy
Relations, and Fine Tuning

- **LF inequalities as monogamy relations**
- **generalisation past GPT-causal models**
 - **d -sep causal models** $(A \perp_d B|C \implies A \perp B|C)$
 - **cyclic causal models**



**Yìlè
Yīng**



**Marina
Maciel Ansanelli**



**Elie
Wolfe**



**David
Schmid**

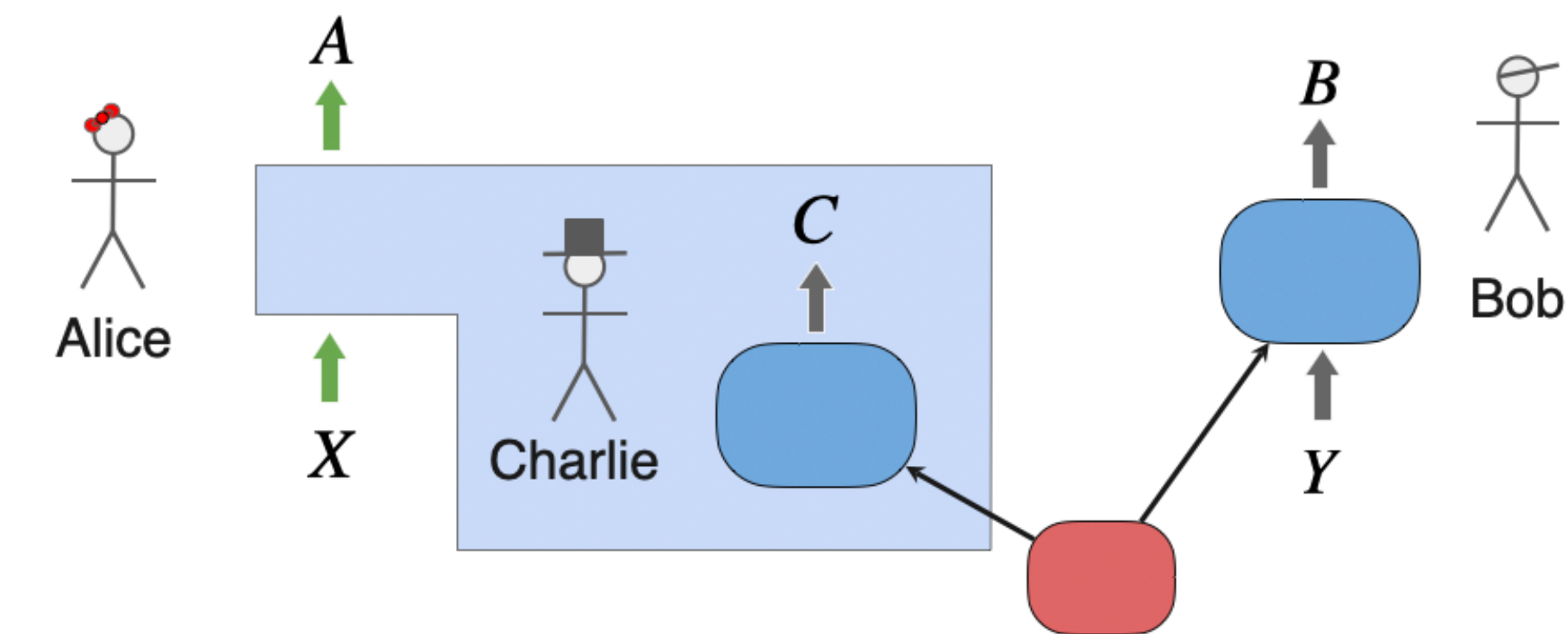


**Eric Gama
Cavalcanti**

**giving up
absoluteness of observed events?**

giving up absoluteness of observed events

relative facts?



absoluteness of
observed events

$$f(ab | xy) = \sum_c p(abc | xy)$$
$$p(a = c | x = 1) = 1$$

arXiv:2402.08727v2 (quant-ph)

[Submitted on 13 Feb 2024 (v1), last revised 20 Jan 2025 (this version, v2)]

**On the significance of Wigner's Friend
in contexts beyond quantum
foundations**

Caroline L. Jones, Markus P. Mueller

Open Access Editor's Choice Article

**Parallel Lives: A Local-Realistic
Interpretation of "Nonlocal" Boxes**

by Gilles Brassard ^{1,2,*} and Paul Raymond-Robichaud ^{1,*}
Entropy **2019**, *21*(1), 87; <https://doi.org/10.3390/e21010087>

disturbance

$$p(a = c | x = 1) \neq 1$$

disturbing Charlie
too much

relative facts

$$f(ab | xy) \neq \sum_c p(abc | xy)$$
$$p(a = c | x = 1) = 1$$

interference sign of relational facts
no sense to ask "what was the value of C ?"
without actually asking Charlie
interference effects delete information

duplication

$$f(ab | xy) \neq \sum_c p(abc | xy)$$

two or more Charlies in the box,
no way to unambiguously
identify *the* value of C

LF violation due to interference
of these two localised worlds

thank you for listening

closing remarks

- EWFS stands to WF like Bell stands to EPR
- EWFS even stronger challenge to causal modelling
 - is there a further generalisation?
- letting go of absoluteness of observed events: what does it mean, exactly?
- violations of LF inequalities already happened, but for small systems
 - what is a good friend?
---> theory of observers

